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# COMPARISON OF SEVERAL METHODS FOR ESTIMATING LOW-SPEED STABILITY DERIVATIVES FOR TWO AIRPLANE CONFIGURATIONS

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## ERRATA

NASA Technical Note D-6531

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By Herman S. Fletcher

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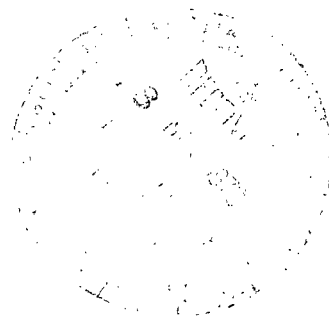
Page 10: Under the section entitled " $C_{l_r}$  (fig. 17)," delete the last sentence:  
"The equation given in reference 4 for the tail contribution to  $C_{l_r}$  appears to have a sign error, which causes the  $C_{l_r}$  value to be too negative."

Then, reword the entire section as follows:

$C_{l_r}$  (fig. 17). - Figure 17 shows that the estimated values of  $C_{l_r}$  were in fair agreement with each other for the unswept- and swept-wing configurations.

Page 33: Replace figure 17 with the attached corrected figure.

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COMPARISON OF SEVERAL METHODS FOR ESTIMATING  
LOW-SPEED STABILITY DERIVATIVES FOR  
TWO AIRPLANE CONFIGURATIONS

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SUMMARY

Methods presented in five different publications have been used to estimate the low-speed stability derivatives of two unpowered airplane configurations. One configuration had unswept lifting surfaces; the other configuration was the D-558-II swept-wing research airplane. The results of the computations were compared with each other, with existing wind-tunnel data, and with flight-test data for the D-558-II configuration to assess the relative merits of the methods for estimating derivatives.

In general, it was found that all the methods gave reasonably accurate predictions for those derivatives which are attributed primarily to the wing and horizontal tail – mainly, the longitudinal derivatives. Even in these instances, however, there was some variation in the estimated horizontal tail and fuselage contribution to the pitching moments.

There were large differences between some of the lateral derivatives computed by using the various estimation methods. Most of the differences can be traced to the estimated vertical-tail effectiveness. A detailed comparison of tail-effectiveness estimates is not feasible because of differences in definitions of effective areas, span, interference effects, and so on.

The results of this study indicate that, in general, for low subsonic speeds, no one text appeared consistently better for estimating all derivatives.

INTRODUCTION

Aerodynamic derivatives of airplanes are required for several types of analyses, such as stability calculations, motion response, and man-machine simulation. In order for the results of such analyses to be valid, it is necessary that the derivatives be accurate. There are three general methods of obtaining aerodynamic derivatives of a complete airplane, and these are

- (1) Analytical methods based on theory and on empirical relations derived from accumulated wind-tunnel data
- (2) Wind-tunnel tests of the airplane or a model of the airplane
- (3) Analysis of flight data

Each of these basic methods is subject to some limitations and interpretations. There are several documents available in which techniques are presented for estimating derivatives (e.g., refs. 1 to 5). There are also several techniques available for extracting derivatives from flight data.

A recent publication (ref. 6) compared the stability derivatives of a Navion aircraft as determined by several textbook methods, from wind-tunnel tests, and from flight data. There were large differences in some of the more important derivatives. The reasons for the differences in some instances were not identified.

The present study was initiated to determine whether there are basic differences in the various published methods, to point out the differences found, and to assess the relative merits of the methods for estimating the low-speed stability derivatives. The study is based on computation by various methods of the derivatives for two specific airplane configurations for which much wind-tunnel data were available. Considerable flight data also were available for one of the configurations. In addition, some other comparisons are available for flight, wind-tunnel, and theoretical derivatives (for example, refs. 7 to 19). However, these references are different in scope and for other airplane configurations than those considered herein.

## SYMBOLS

The calculated, experimental, and flight-extracted derivatives are presented in the form of standard NASA coefficients and moments about the stability axes. Values are given in both SI and U.S. Customary Units. The measurements and calculations were made in U.S. Customary Units. The coefficients and symbols used herein are defined as follows:

|            |   |
|------------|---|
| b          | span, meters (feet)   |
| $\bar{c}$  | mean aerodynamic chord, meters (feet)   |
| $q_V$      | dynamic pressure at vertical tail, newtons per meter <sup>2</sup> (pounds per foot <sup>2</sup> ) |
| $q_\infty$ | free-stream dynamic pressure, newtons per meter <sup>2</sup> (pounds per foot <sup>2</sup> )      |
| S          | wing area, meters <sup>2</sup> (feet <sup>2</sup> )   |

|                                |  |
|--------------------------------|--|
| $t$                            | time, seconds  |
| $\alpha$                       | angle of attack of body reference line, radians                      |
| $\dot{\alpha} = d\alpha/dt$    |  |
| $\beta$                        | sideslip angle, $\sin^{-1} \frac{v}{V_{\infty}}$ , radians           |
| $d\epsilon/d\alpha$            | change in downwash angle with angle of attack                        |
| $\partial\sigma/\partial\beta$ | change in sidewash angle at tail with change in sideslip angle       |
| $M$                            | Mach number  |
| $p$                            | rolling velocity, radians per second                                 |
| $q$                            | pitching velocity, radians per second                                |
| $r$                            | yawing velocity, radians per second                                  |
| $V_{\infty}$                   | free-stream velocity, meters per second (feet per second)            |
| $v$                            | velocity along Y-axis, meters per second (feet per second)           |
| $pb/2V_{\infty}$               | wing-tip helix angle, radians  |
| $rb/2V_{\infty}$               | yawing-angular-velocity parameter, radians                           |
| $F_L$                          | lift, newtons (pounds)   |
| $F_Y$                          | side force, newtons (pounds)   |
| $M_X$                          | rolling moment, meter-newtons (foot-pounds)                          |
| $M_Y$                          | pitching moment about center of gravity, meter-newtons (foot-pounds) |
| $M_Z$                          | yawing moment, meter-newtons (foot-pounds)                           |
| $C_L$                          | lift coefficient, $F_L/q_{\infty}S$                                  |

- $C_l$  rolling-moment coefficient,  $M_X/q_\infty S b$
- $C_m$  pitching-moment coefficient,  $M_Y/q_\infty S \bar{c}$
- $C_n$  yawing-moment coefficient,  $M_Z/q_\infty S b$
- $C_Y$  side-force coefficient,  $F_Y/q_\infty S$
- $C_{L\alpha}$  lift-curve slope,  $\partial C_L/\partial \alpha$ , per radian
- $C_{m\alpha}$  pitching-moment-curve slope,  $\partial C_m/\partial \alpha$ , per radian
- $C_{m\dot{\alpha}}$  angle-of-attack damping parameter,  $\partial C_m/\partial \frac{\dot{\alpha} \bar{c}}{2V_\infty}$ , per radian
- $C_{l\beta}$  rolling moment due to sideslip or effective-dihedral parameter,  $\partial C_l/\partial \beta$ , per radian
- $C_{n\beta}$  yawing moment due to sideslip or directional-stability parameter,  $\partial C_n/\partial \beta$ , per radian
- $C_{Y\beta}$  side force due to sideslip,  $\partial C_Y/\partial \beta$ , per radian
- $C_{mq}$  damping-in-pitch parameter,  $\partial C_m/\partial \frac{q \bar{c}}{2V_\infty}$ , per radian
- $C_{mq} + C_{m\dot{\alpha}}$  effective damping-in-pitch parameter, per radian
- $C_{lp}$  rolling moment due to rolling velocity or damping-in-roll parameter,  $\partial C_l/\partial \frac{pb}{2V_\infty}$ , per radian
- $C_{np}$  yawing moment due to rolling velocity or adverse-yaw parameter,  $\partial C_n/\partial \frac{pb}{2V_\infty}$ , per radian
- $C_{Yp}$  side force due to rolling velocity,  $\partial C_Y/\partial \frac{pb}{2V_\infty}$ , per radian
- $C_{lr}$  rolling moment due to yawing velocity,  $\partial C_l/\partial \frac{rb}{2V_\infty}$ , per radian
- $C_{nr}$  yawing moment due to yawing velocity or damping-in-yaw parameter,  $\partial C_n/\partial \frac{rb}{2V_\infty}$ , per radian

$C_{Y_r}$  side force due to yawing velocity,  $\partial C_Y / \partial \frac{rb}{2V_\infty}$ , per radian

Subscript:

V vertical tail

Model component designations:

W wing

WF wing-fuselage

V vertical tail

H horizontal tail

WVH complete model or airplane

## AIRPLANE CONFIGURATIONS

The airplane configurations selected for this study are shown in figures 1 and 2. Figure 1 is a drawing of the general research model which was used in several wind-tunnel studies as part of a series of investigations to determine the effects of airplane geometry on stability derivatives. Figure 2 is a drawing of the D-558-II swept-wing airplane. Much wind-tunnel data from model tests and some flight data obtained with the full-scale airplanes are available for comparison with estimated derivatives. The two configurations vary appreciably from each other in geometric appearance, which is desirable for this type of analysis. Some of the pertinent geometric characteristics of the two configurations are presented in table I.

## SCOPE OF THE STUDY

The computation of aerodynamic stability derivatives was limited to low angles of attack ( $5.73^\circ$  for the unswept-wing model and  $4^\circ$  for the swept-wing model) and low subsonic Mach number ( $M \approx 0.16$ ). The derivatives computed were those listed in the section "Symbols" and are those generally considered to be important in aircraft dynamics. The procedures given in three well-known textbooks (refs. 1, 3, and 4), in an NACA Report (ref. 2), and in a U.S. Air Force sponsored publication (ref. 5) were followed in making the calculations. The experimental data used in conjunction with reference 2



were taken from reference 20. Results of the calculations are compared with wind-tunnel data and also with flight data for the D-558-II swept-wing configuration.

### PRESENTATION OF RESULTS

The results of this study are presented in a series of charts which compare estimates of parameters as obtained from application of various published methods (refs. 1 to 5) and from wind-tunnel and flight data (refs. 20 to 26). All the data from wind-tunnel and flight test experiments are shown as solid symbols with those representing the flight test data being flagged. In some cases, estimated parameters are shown for various combinations of components to try to identify reasons why the analytical methods yield appreciably different results. The data are presented in the figures as shown in the following table:

| Parameter                              | Figure |
|--|--------|
| $C_{L\alpha}$ . . . . .                | 3      |
| $C_{m\alpha}$ . . . . .                | 4      |
| $d\epsilon/d\alpha$ . . . . .          | 5      |
| $C_{mq}$ . . . . .                     | 6      |
| $C_{m\dot{\alpha}}$ . . . . .          | 7      |
| $C_{mq} + C_{m\dot{\alpha}}$ . . . . . | 8      |
| $C_{Y\beta}$ . . . . .                 | 9      |
| $C_{n\beta}$ . . . . .                 | 10     |
| $C_{l\beta}$ . . . . .                 | 11     |
| $C_{Yp}$ . . . . .                     | 12     |
| $C_{np}$ . . . . .                     | 13     |
| $C_{lp}$ . . . . .                     | 14     |
| $C_{Yr}$ . . . . .                     | 15     |
| $C_{nr}$ . . . . .                     | 16     |
| $C_{lr}$ . . . . .                     | 17     |

## RESULTS AND DISCUSSION

The results are discussed in two separate sections: one related to longitudinal derivatives and the other to lateral derivatives. The wind-tunnel data are used as a basis for comparison of the results obtained by the various methods of estimating derivatives. The comparisons are first made for the complete airplane configuration. If the agreement between estimates and wind-tunnel results is poor, additional comparisons are made for various components of the configurations to try to identify the factors responsible for the differences.

### Longitudinal Derivatives

$C_{L\alpha}$  (fig. 3).- The estimated values of  $C_{L\alpha}$  were within 10 percent of the wind-tunnel results (refs. 21, 22, and 23). (See fig. 3.) The wing is the primary contributor to this parameter, and the differences in estimates obtained from the various references can be traced to differences in the wing contribution. These can, in turn, be associated with small differences in suggested values of section lift-curve slope, neglect of taper-ratio effects, or the form of the equation for  $C_{L\alpha}$ . It appears that all the methods used were about equally good for the two configurations of this study and that reference 5 was the best for the swept-wing configuration as is evident from a comparison of wind-tunnel data (refs. 22 and 23) and flight test data (ref. 24). It also appears from unpublished calculations that the smaller total  $C_{L\alpha}$  values obtained for the swept-wing configuration by using references 1 to 4 are due partly to neglect of or incorrect wing-fuselage effects.

$C_{m\alpha}$  (fig. 4).- All except reference 4 of the analytical methods predicted a small stable (negative) value of  $C_{m\alpha}$  for the unswept-wing configuration. (See fig. 4(a).) The wind-tunnel value was a small positive value. However, the data source (ref. 21) indicated that the experimental value probably was in error because of geometric asymmetries and should have been neutrally stable ( $C_{m\alpha} = 0$ ). The range of computed values of  $C_{m\alpha}$  was from about 0.07 to -0.13 (fig. 4(a)), which corresponds to a static-margin range of from about -0.02 to 0.03. This range is quite reasonable, and it appears that all the computational methods were equally good for the unswept-wing configuration.

The estimated values of  $C_{m\alpha}$  for the complete swept-wing configuration varied from -0.42 to -0.87. The wind-tunnel (ref. 23) and flight-extracted values (ref. 24) were about -0.65. Since there was such a large spread in the calculated values, additional curves are shown in figure 4(b) to isolate the causes of the differences. It can be seen that the primary causes of the differences are in the estimated values of the fuselage and horizontal-tail contributions to  $C_{m\alpha}$ . Additional factors which are not readily apparent in figure 4(b) but which also have some effect are differences in downwash (fig. 5) and

interference factors. The value estimated by use of reference 3 came closest to the wind-tunnel and flight-test values (fig. 4(b)).

$C_{m_q}$  (fig. 6).- The primary contribution to  $C_{m_q}$  comes from the horizontal tail, and a small increment is produced by the wing. The analytical methods of references 1 to 5 are all approximately the same when nondimensionalized in the same manner and, therefore, yield comparable results. Differences which do occur are associated with suggested values of section lift-curve slope or neglecting taper-ratio effects in estimating the horizontal-tail lift-curve slope. Interference effects, however, are responsible for the poor agreement for the swept wing by using reference 5. (See fig. 6.) There were no experimental values available for comparison with the estimated values.

$C_{m_{\dot{\alpha}}}$  (fig. 7).- The primary contribution to  $C_{m_{\dot{\alpha}}}$  comes from the horizontal tail also. Since all the analytical methods used herein were based on the same reference, they all yielded approximately the same result. (See fig. 7.) There were no experimental values available for comparison with estimated values.

$C_{m_q} + C_{m_{\dot{\alpha}}}$  (fig. 8).- The sum of the derivatives  $C_{m_q}$  and  $C_{m_{\dot{\alpha}}}$  is the effective damping-in-pitch parameter. For this study the computed values of the component coefficients (from figs. 6 and 7) were simply added. The combination parameter can be obtained experimentally from the rate of damping of an oscillation about the Y body axis. There were no experimental data available for the unswept-wing configuration; however, there was a source of values for the swept-wing configuration. These data were for free-flight tests with a model at  $M = 0.6$  (ref. 25). The results from the model tests are in good agreement with the computations. (See fig. 8.)

#### Lateral Derivatives

$C_{Y_\beta}$  (fig. 9).- The calculated data show large differences in the values of  $C_{Y_\beta}$  as estimated by the methods of the various references. (See fig. 9.) The following factors account for the major differences in the values obtained by the various methods.

Reference 1: (a) No procedure is given to account for the end-plate effect of the fuselage on the vertical-tail effectiveness. (b) No procedure is given to account for the fuselage contribution to  $C_{Y_\beta}$ . (c) No procedure is given to account for the effect of the horizontal tail on the vertical tail (end-plate effect) if the horizontal tail is located somewhere other than at the base of the vertical tail.

Reference 3: No procedure is given to account for any fuselage contribution to  $C_{Y_\beta}$ .

Reference 4: (a) No method is given to estimate the end-plate effect of the blunt-tail fuselage on the aspect ratio of the vertical tail. (b) No procedure is given to estimate the

end-plate effect of the horizontal tail on the vertical tail for a position of the horizontal tail other than at the extremities of the vertical tail.

$C_{n\beta}$  (fig. 10).- There was a rather wide range in estimated values of  $C_{n\beta}$  for both airplane configurations. (See fig. 10.) Most of the differences are associated with the estimated contribution of the vertical tail to  $C_{n\beta}$ . The low value obtained from the use of reference 4 for the swept-wing configuration is caused primarily by not properly accounting for the effects of the fuselage and horizontal tail on the lift-curve slope of the vertical tail.

$C_{l\beta}$  (fig. 11).- The values of  $C_{l\beta}$  estimated by use of references 3, 4, and 5 are much higher (more negative) than the wind-tunnel value (ref. 21) or the values estimated by use of references 1 and 2 for the unswept-wing configuration. The estimated tail contribution exceeds the wing contribution, and the differences in estimated tail contributions are primarily responsible for the differences in  $C_{l\beta}$  of the various estimates.

The estimated values of  $C_{l\beta}$  for the swept-wing configuration vary over a large range. The reasons for the differences in computed values in this case can be identified quite readily as follows.

Reference 1: It is perhaps unfair to include an estimate of  $C_{l\beta}$  for the swept-wing configuration from reference 1. The difficulty lies in the fact that although reference 1 discusses the importance of wing sweep on  $C_{l\beta}$ , it gives no procedure for estimating this important effect.

Reference 4: The estimated value of  $C_{l\beta}$  for the swept-wing configuration is somewhat low, primarily because the end-plate effects of the body and horizontal tail on the vertical tail are neglected.

$C_{Y_p}$  (fig. 12).- Although  $C_{Y_p}$  itself is not of much importance in determining the dynamics of an airplane, it is important for correcting the other rolling derivatives if the center of gravity is changed. The total estimated values of  $C_{Y_p}$  for the unswept-wing configuration are generally less positive than the experimental value (ref. 21). (See fig. 12.) Most of this difference is caused by the estimated contribution of the vertical tail. The computations indicate a small positive increment due to the vertical tail, whereas the experimental data indicate a rather large positive increment. The estimated  $C_{Y_p}$  values of the swept-wing configuration are in very good agreement with experimental data (ref. 22).

$C_{n_p}$  (fig. 13).- The estimated values of  $C_{n_p}$  were in reasonably good agreement with the experimental values (refs. 21 and 22) for the unswept-wing and for the swept-wing configurations. (See fig. 13.)

$C_{l_p}$  (fig. 14).- The primary contribution to  $C_{l_p}$  comes from the wing. Application of references 2, 3, 4, and 5 results in underestimating the unswept-wing contribution to  $C_{l_p}$ , and thereby also underestimating the total  $C_{l_p}$  of the unswept-wing configuration. (See fig. 14.) Extrapolation of the  $C_{l_p}$  curves given in reference 1 yields a value of  $C_{l_p}$  which is in good agreement with experimental data (refs. 21 and 22). All the methods yielded estimates of  $C_{l_p}$  for the swept-wing configuration which were very close to the experimental value (refs. 21, 22, and 24).

$C_{Y_r}$  (fig. 15).- The parameter  $C_{Y_r}$  is generated almost totally by the vertical tail. References 1 and 4 did not present a specific method for computing  $C_{Y_r}$ ; however, an estimate is readily obtainable from the  $C_{n_r}$  equations that are presented. There are no experimental data available for the unswept-wing configuration for comparison with the calculations. The computed results for the swept-wing configuration generally are greater than the experimental values (ref. 22), particularly the value estimated by using reference 5. (See fig. 15.) The large swept-wing value for reference 5 is primarily caused by  $\left(1 + \frac{\partial \sigma}{\partial \beta}\right) \frac{qV}{q_\infty}$  used in the  $(C_{Y_\beta})_V$  expression.

$C_{n_r}$  (fig. 16).- The methods of references 1, 2, 3, and 5 yielded reasonably good estimates of  $C_{n_r}$  when compared with wind-tunnel data (refs. 22 and 26). (See fig. 16.) The omission of blunt-body end-plate effect on the vertical tail for reference 4 resulted in a large error for the tail contribution to  $C_{n_r}$  for the swept-wing configuration.

$C_{l_r}$  (fig. 17).- Figure 17 shows that the estimated values of  $C_{l_r}$  were in fair agreement with each other for the unswept- and swept-wing configurations.

#### CONCLUDING REMARKS

Methods presented in five different publications have been used to estimate the low-speed aerodynamic derivatives of two unpowered airplane configurations. One configuration had unswept lifting surfaces, the other configuration was the D-558-II swept-wing research airplane. The results of the computations were compared with each other, with existing wind-tunnel data, and with flight-test data for the D-558-II configuration to assess the relative merits of the methods for estimating derivatives.

In general, it was found that all the methods gave reasonably accurate predictions for those derivatives which are attributed primarily to the wing and horizontal tail - mainly, the longitudinal derivatives. Even in these instances, however, there was some variation in the estimated horizontal tail and fuselage contribution to the pitching moments.

There were large differences between some of the lateral derivatives computed by using the various estimation methods. Most of the differences can be traced to the estimated vertical-tail effectiveness. A detailed comparison of tail-effectiveness estimates is not feasible because of differences in definitions of effective areas, span, interference effects, and so on.

The results of this study indicate that, in general, for low subsonic speeds, no one text appeared consistently better for estimating all derivatives.

Langley Research Center,  
National Aeronautics and Space Administration,  
Hampton, Va. October 14, 1971.

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**TABLE I.- GEOMETRIC CHARACTERISTICS OF CONFIGURATIONS**  
 [Center of gravity at quarter-chord of mean aerodynamic chord]

(a) Unswept-wing model

Wing:

|   |               |
|---|---------------|
| Aspect ratio . . . . .                            | 4.000         |
| Taper ratio . . . . .                             | 0.600         |
| Quarter-chord sweep angle, deg . . . . .          | 0.000         |
| Incidence angle, deg . . . . .                    | 0.000         |
| Dihedral angle, deg . . . . .                     | 0.000         |
| Twist angle, deg . . . . .                        | 0.000         |
| Airfoil section . . . . .                         | NACA 65A008   |
| Area, m <sup>2</sup> (ft <sup>2</sup> ) . . . . . | 0.209 (2.250) |
| Span, m (ft) . . . . .                            | 0.914 (3.000) |
| Mean aerodynamic chord, m (ft) . . . . .          | 0.233 (0.765) |

Vertical tail:

|   |               |
|---|---------------|
| Aspect ratio . . . . .  | 2.000         |
| Taper ratio . . . . .   | 0.600         |
| Quarter-chord sweep angle, deg . . . . .  | 0.000         |
| Airfoil section . . . . .   | NACA 65A008   |
| Area, m <sup>2</sup> (ft <sup>2</sup> ) . . . . .   | 0.031 (0.337) |
| Span, m (ft) . . . . .  | 0.250 (0.821) |
| Mean aerodynamic chord, m (ft) . . . . .  | 0.128 (0.419) |
| Longitudinal distance from center of gravity<br>to vertical tail center of pressure, m (ft) . . . . . | 0.391 (1.282) |
| Vertical distance from center of gravity<br>to vertical tail center of pressure, m (ft) . . . . .     | 0.114 (0.376) |

Horizontal tail:

|   |                |
|---|----------------|
| Aspect ratio . . . . .                            | 4.000          |
| Taper ratio . . . . .                             | 0.600          |
| Quarter-chord sweep angle, deg . . . . .          | 0.000          |
| Incidence angle, deg . . . . .                    | 0.010          |
| Twist angle, deg . . . . .                        | 0.000          |
| Airfoil section . . . . .                         | NACA 65A008    |
| Area, m <sup>2</sup> (ft <sup>2</sup> ) . . . . . | 0.0418 (0.450) |
| Span, m (ft) . . . . .                            | 0.409 (1.342)  |
| Mean aerodynamic chord, m (ft) . . . . .          | 0.104 (0.342)  |
| Tail length, m (ft) . . . . .                     | 0.3907 (1.282) |

Fuselage:

|                          |                |
|--------------------------|----------------|
| Length, m (ft) . . . . . | 1.0158 (3.333) |
| Fineness ratio . . . . . | 6.670          |

**TABLE I.- GEOMETRIC CHARACTERISTICS OF CONFIGURATIONS – Concluded**  
 [Center of gravity at quarter-chord of mean aerodynamic chord]

(b) Swept-wing (D-558-II) model

Wing:

|   |                 |
|---|-----------------|
| Aspect ratio . . . . .  | 3.57            |
| Taper ratio . . . . .   | 0.57            |
| 30-percent-chord sweep angle, deg . . . . .                                 | 35.00           |
| Incidence angle, deg . . . . .  | 3.00            |
| Dihedral angle, deg . . . . .   | -3.00           |
| Twist angle, deg . . . . .  | 0.00            |
| Airfoil section, root . . . . .   | NACA 63010      |
| Airfoil section, tip . . . . .  | NACA 63012      |
| Area, m <sup>2</sup> (ft <sup>2</sup> ) . . . . .                           | 16.258 (175.00) |
| Span, m (ft) . . . . .  | 7.62 (25.00)    |
| Mean aerodynamic chord, m (ft) . . . . .                                    | 2.2159 (7.27)   |
| Leading edge of $\bar{c}$ from leading edge of root chord, m (ft) . . . . . | 1.3746 (4.51)   |
| Spanwise location of $\bar{c}$ from root chord, m (ft) . . . . .            | 1.7068 (5.61)   |

Vertical tail:

|   |               |
|---|---------------|
| Aspect ratio . . . . .  | 1.14          |
| Effective aspect ratio . . . . .                                      | 1.38          |
| Taper ratio . . . . .   | 0.18          |
| 30-percent-chord sweep angle, deg . . . . .                           | 49.00         |
| Airfoil section, root . . . . .                                       | NACA 63010    |
| Airfoil section, tip . . . . .  | NACA 63010    |
| Area to body center line, m <sup>2</sup> (ft <sup>2</sup> ) . . . . . | 5.4626 (58.8) |
| Area of dorsal fin, m <sup>2</sup> (ft <sup>2</sup> ) . . . . .       | 0.464 (5.0)   |
| Span from fuselage center line, m (ft) . . . . .                      | 2.487 (8.16)  |
| Mean aerodynamic chord (excluding dorsal fin), m (ft) . . . . .       | 2.575 (8.45)  |
| Tip chord (parallel to body center line), m (ft) . . . . .            | 0.676 (2.22)  |
| Root chord (parallel to body center line), m (ft) . . . . .           | 3.758 (12.33) |
| Longitudinal distance from center of gravity                          |               |
| to vertical tail center of pressure, m (ft) . . . . .                 | 5.124 (16.81) |
| Vertical distance from center of gravity                              |               |
| to vertical tail center of pressure, m (ft) . . . . .                 | 1.0668 (3.5)  |

Horizontal tail:

|   |                |
|---|----------------|
| Aspect ratio . . . . .                              | 3.59           |
| Taper ratio . . . . .                               | 0.50           |
| 30-percent-chord sweep angle, deg . . . . .         | 40.00          |
| Dihedral angle, deg . . . . .                       | 0.00           |
| Airfoil section, root . . . . .                     | NACA 63010     |
| Airfoil section, tip . . . . .                      | NACA 63010     |
| Area, m <sup>2</sup> (ft <sup>2</sup> ) . . . . .   | 3.7068 (39.90) |
| Span, m (ft) . . . . .                              | 3.642 (11.95)  |
| Mean aerodynamic chord, m (ft) . . . . .            | 1.0607 (3.48)  |
| Height above fuselage center line, m (ft) . . . . . | 1.295 (4.25)   |
| Tail length, m (ft) . . . . .                       | 5.916 (19.41)  |
| Tip chord, m (ft) . . . . .                         | 0.6797 (2.23)  |

Fuselage:

|                          |                 |
|--------------------------|-----------------|
| Length, m (ft) . . . . . | 12.8016 (42.00) |
| Fineness ratio . . . . . | 8.40            |

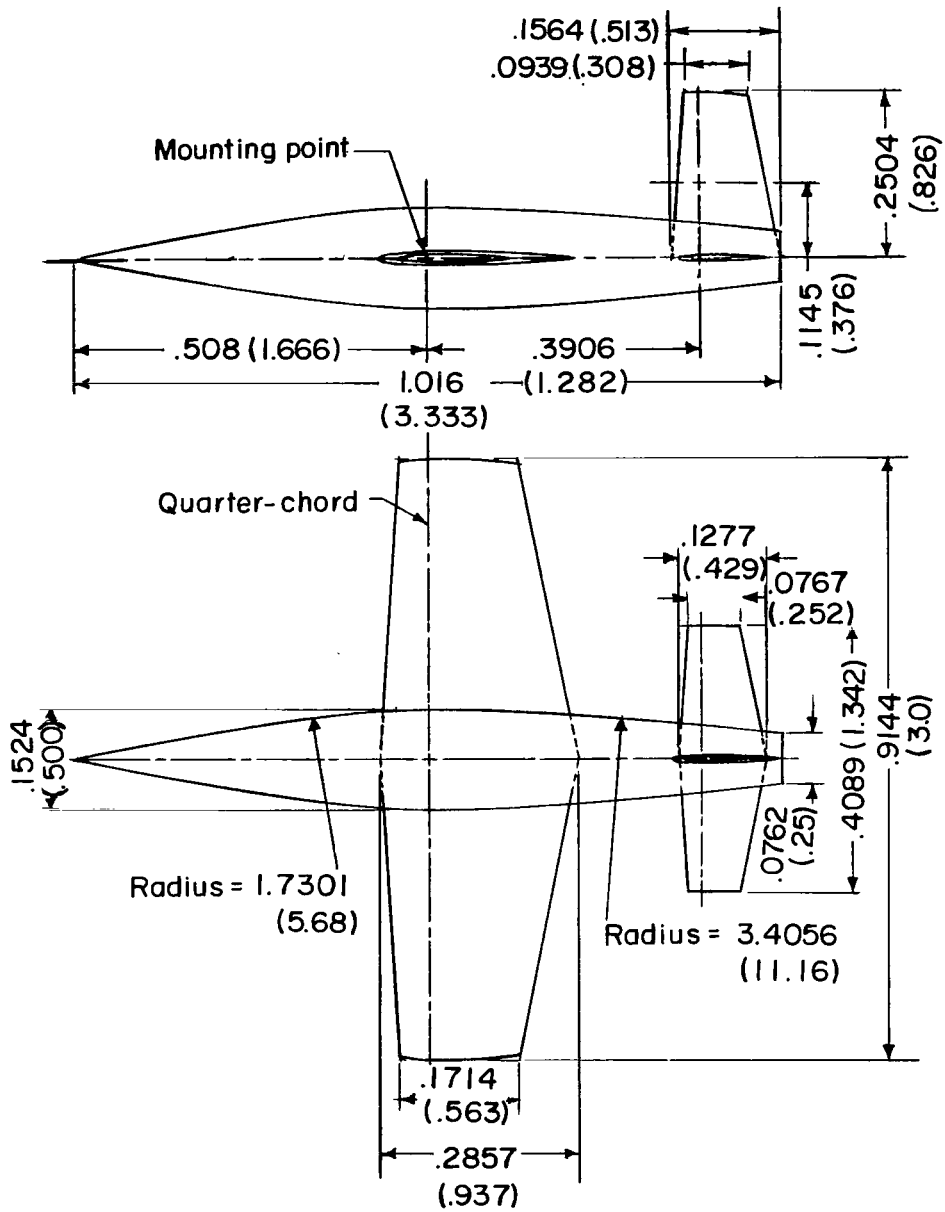


Figure 1.- Drawing of unswept-wing model. All dimensions are in meters (feet).

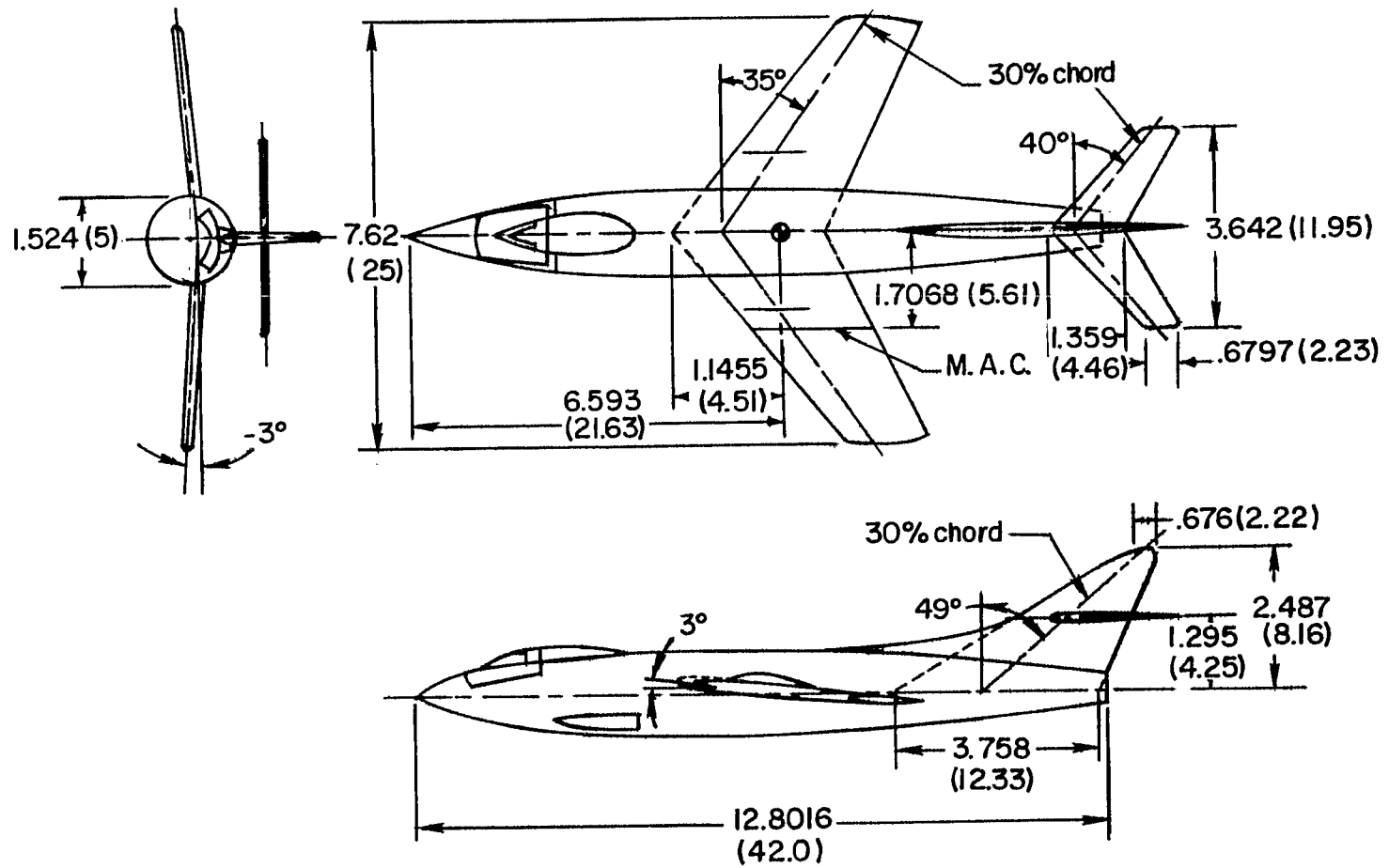


Figure 2.- Drawing of D-558-II swept-wing research airplane. All dimensions are in meters (feet).

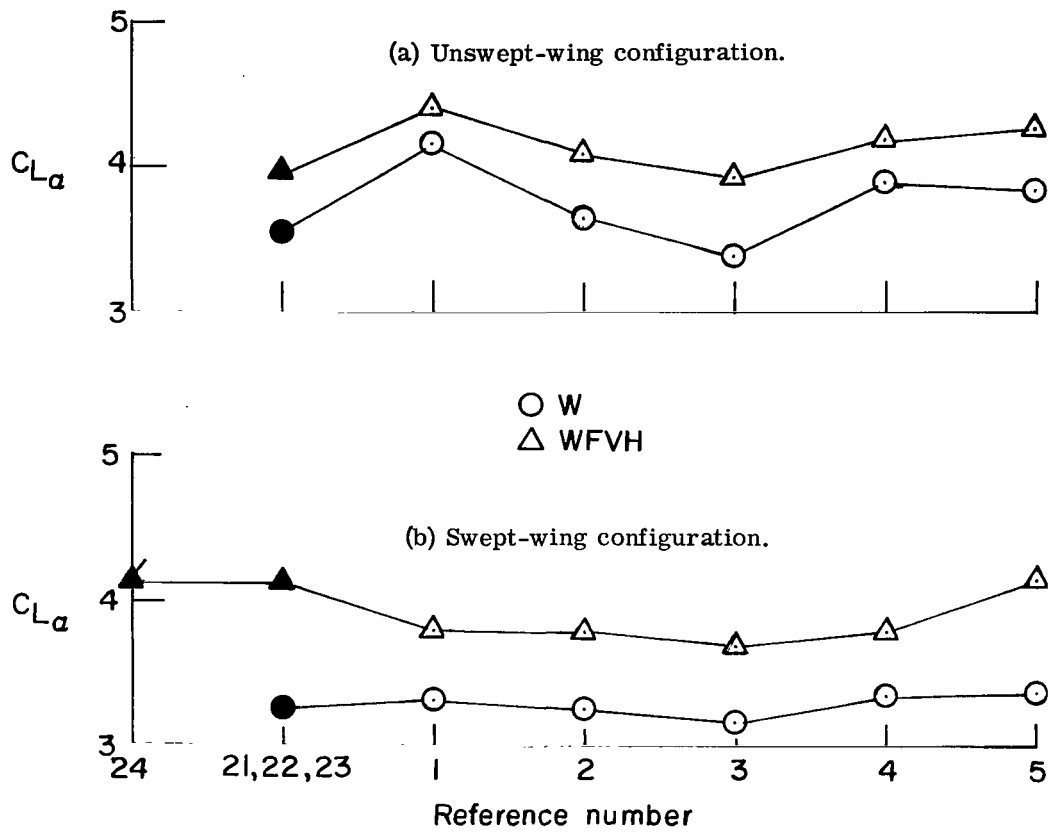


Figure 3.- Lift-curve slope. Solid symbols indicate experimental data; flagged symbol indicates flight test.

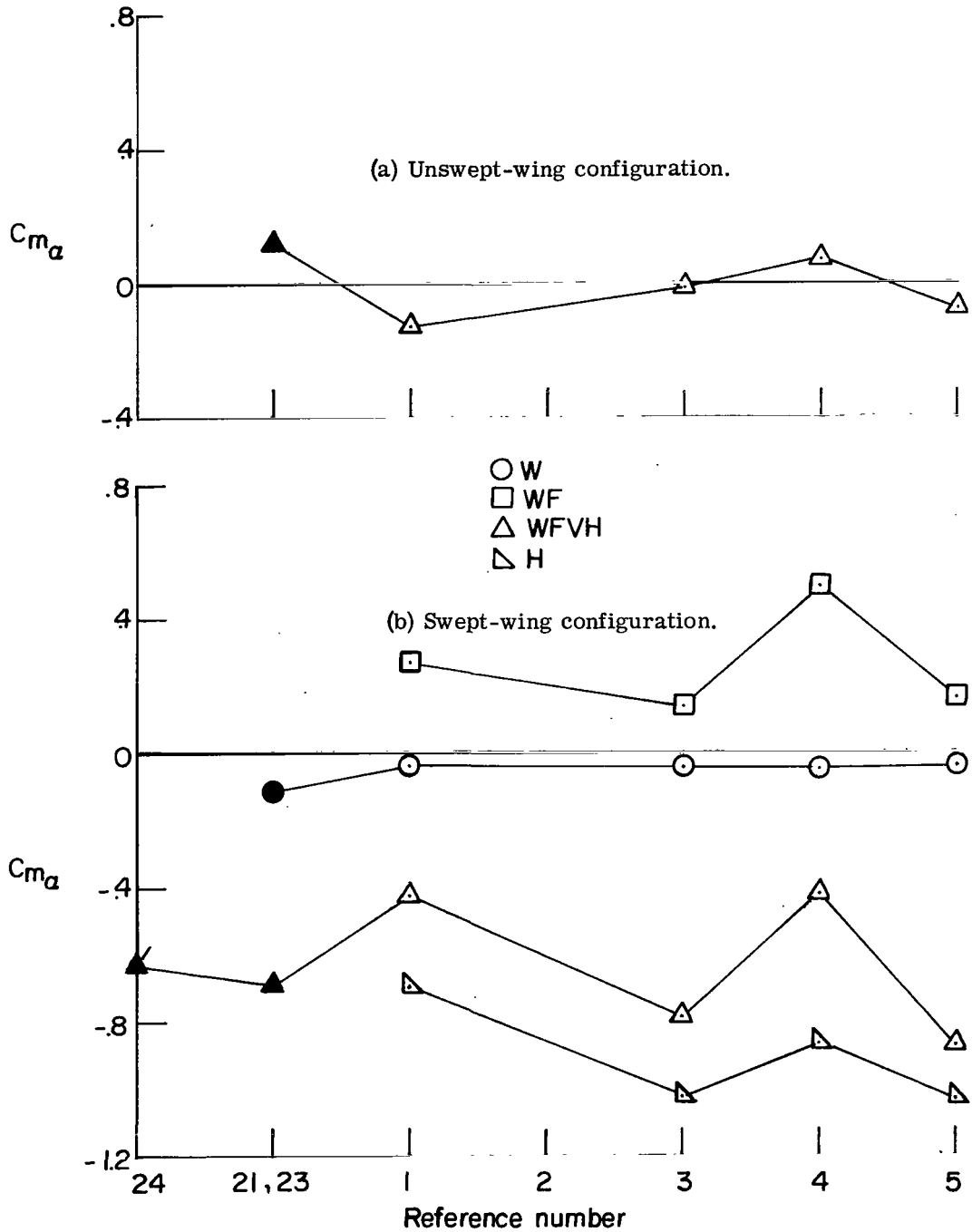


Figure 4.- Static longitudinal stability parameter. Solid symbols indicate experimental data; flagged symbol indicates flight test.

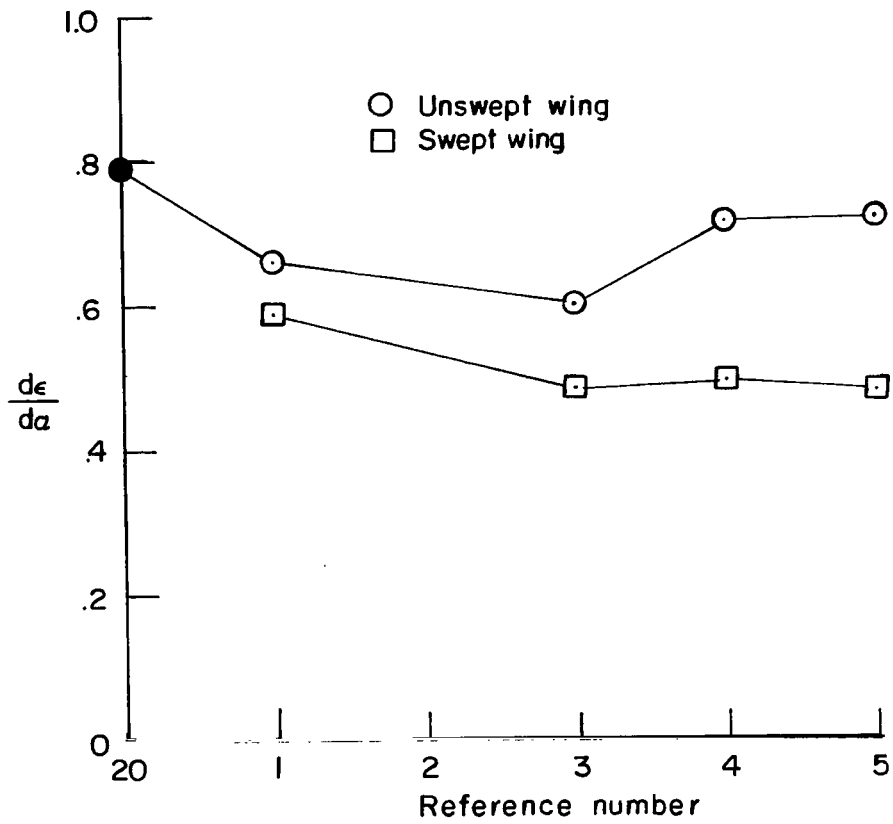


Figure 5.- Downwash parameter. Solid symbol indicates experimental data.

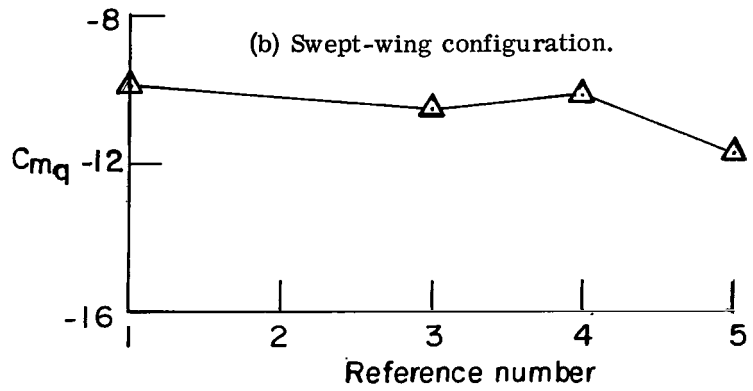
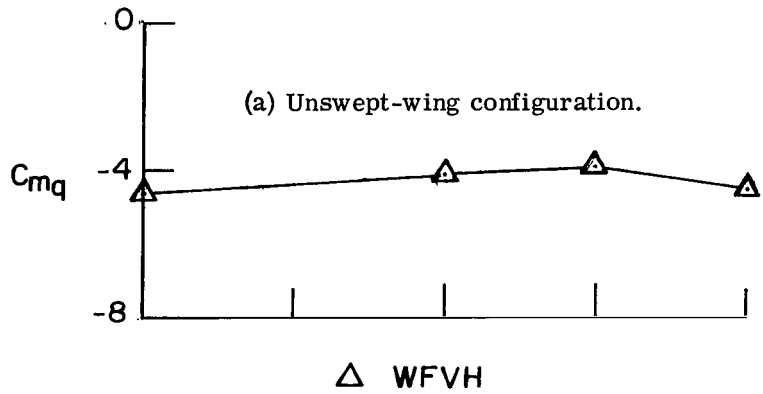


Figure 6.- Pitching moment due to pitching velocity or damping-in-pitch parameter.

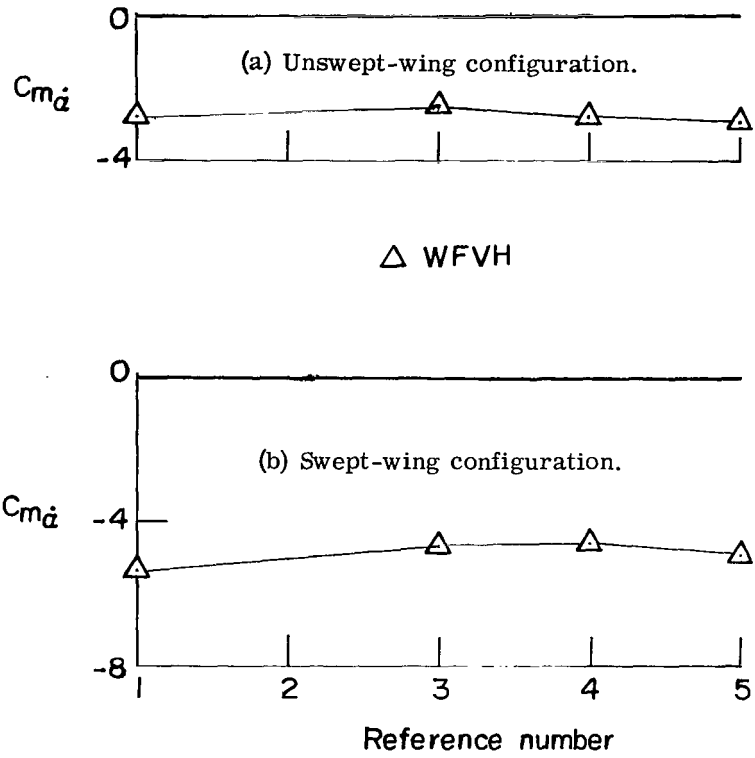


Figure 7.- Angle-of-attack damping parameter.

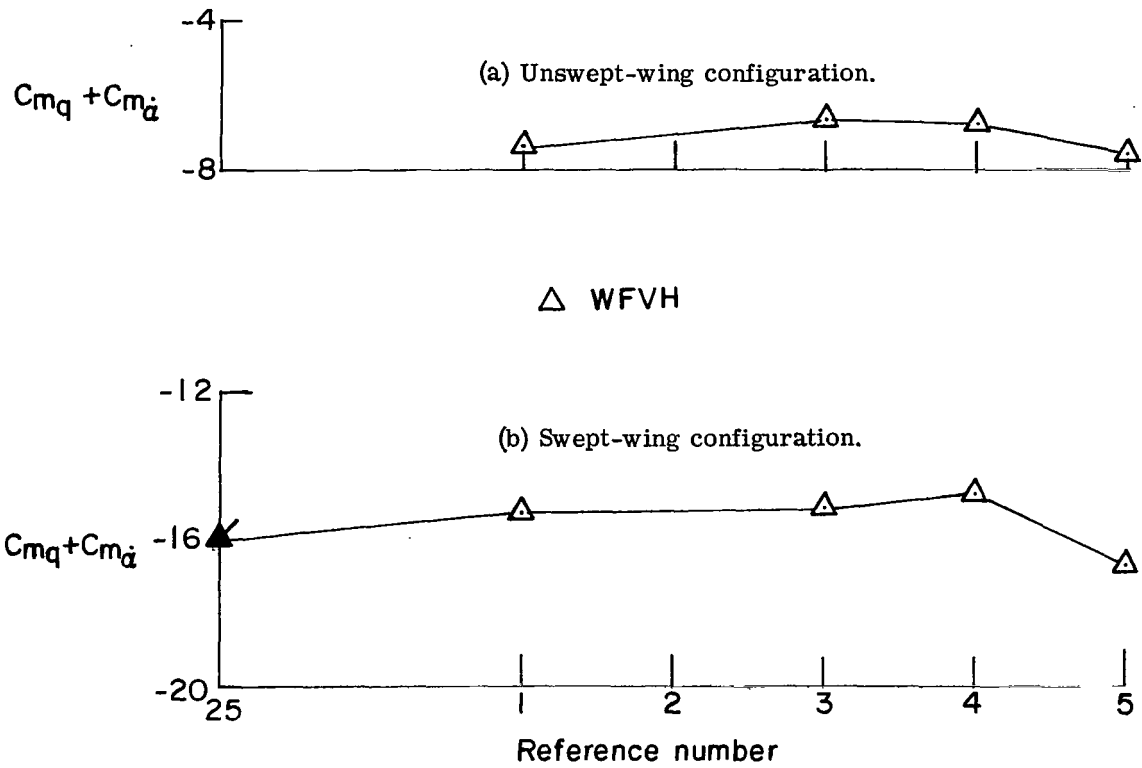


Figure 8.- Effective damping-in-pitch parameter. Solid flagged symbol indicates flight test data.

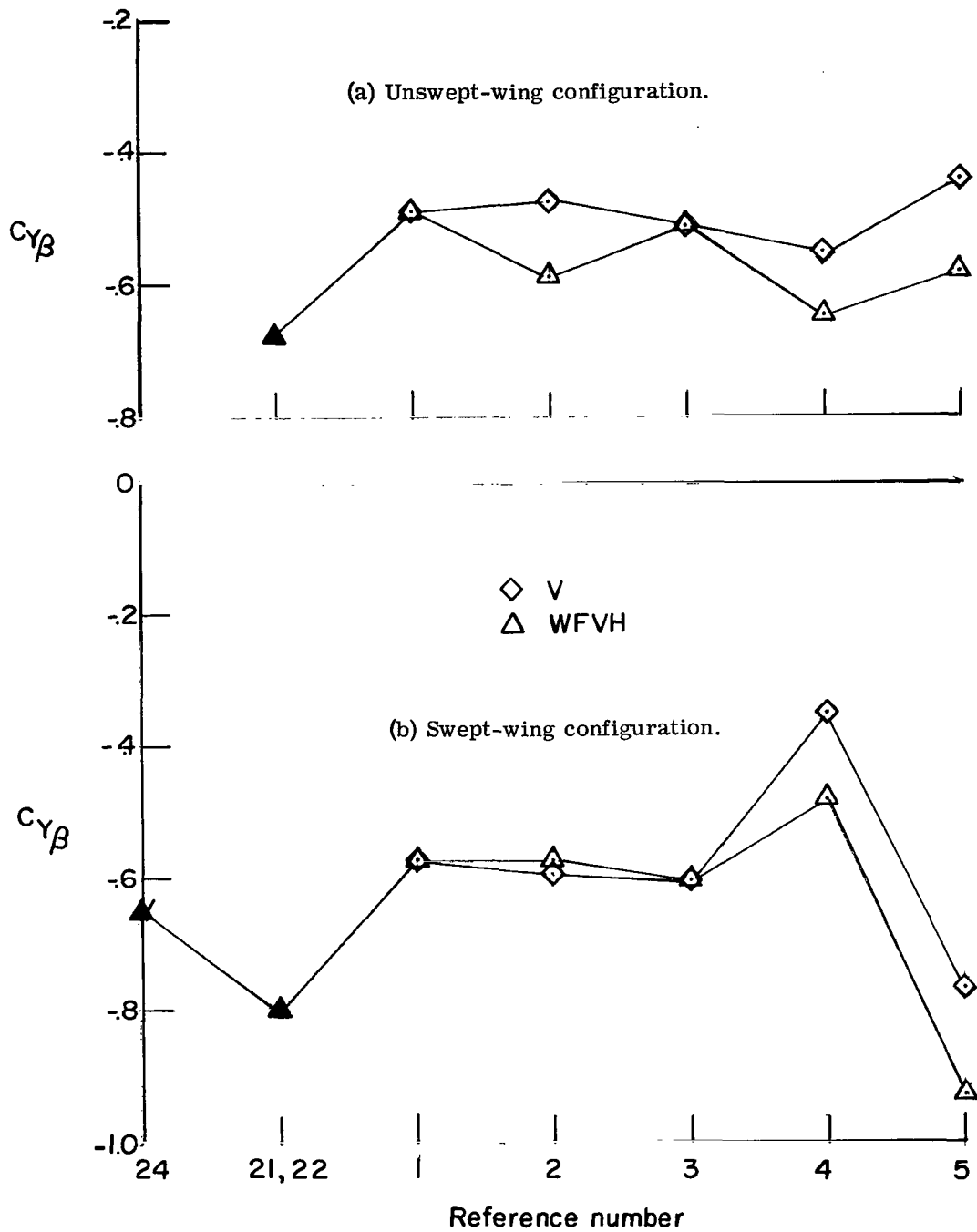


Figure 9.- Side force due to sideslip. Solid symbols indicate experimental data; flagged symbol indicates flight test.

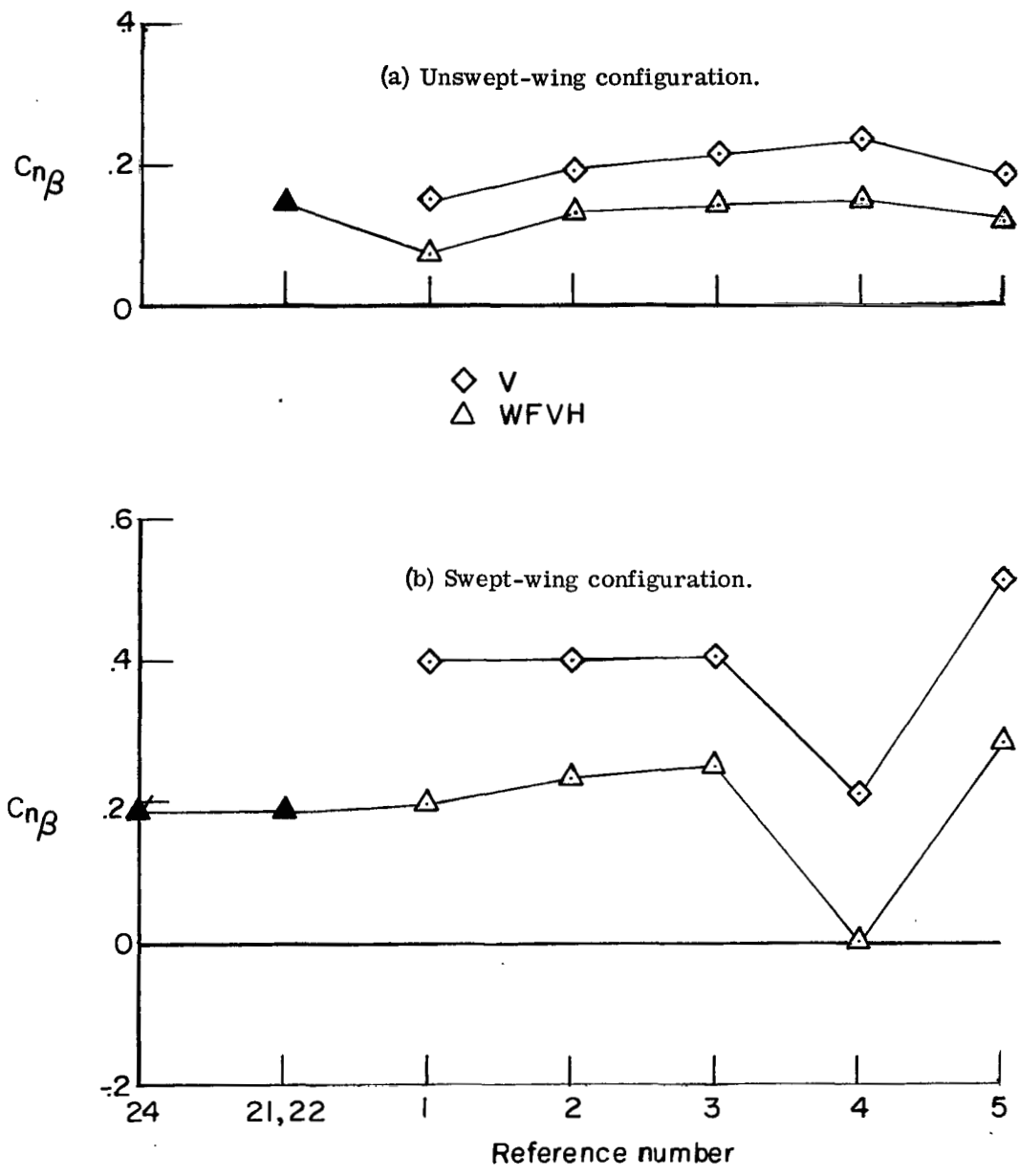


Figure 10.- Yawing moment due to sideslip. Solid symbols indicate experimental data; flagged symbol indicates flight test.

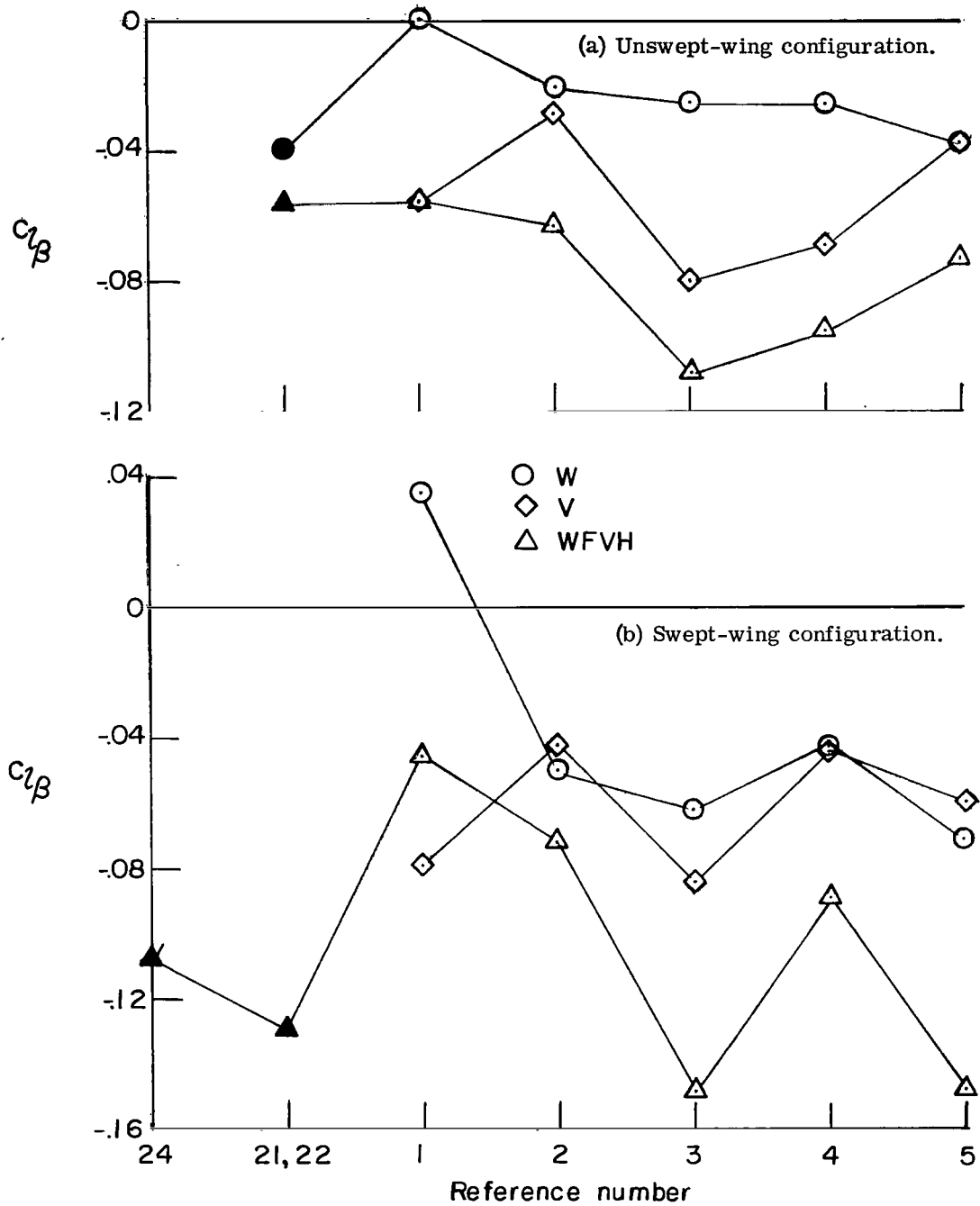


Figure 11.- Rolling moment due to sideslip or effective-dihedral parameter. Solid symbols indicate experimental data; flagged symbol indicates flight test.

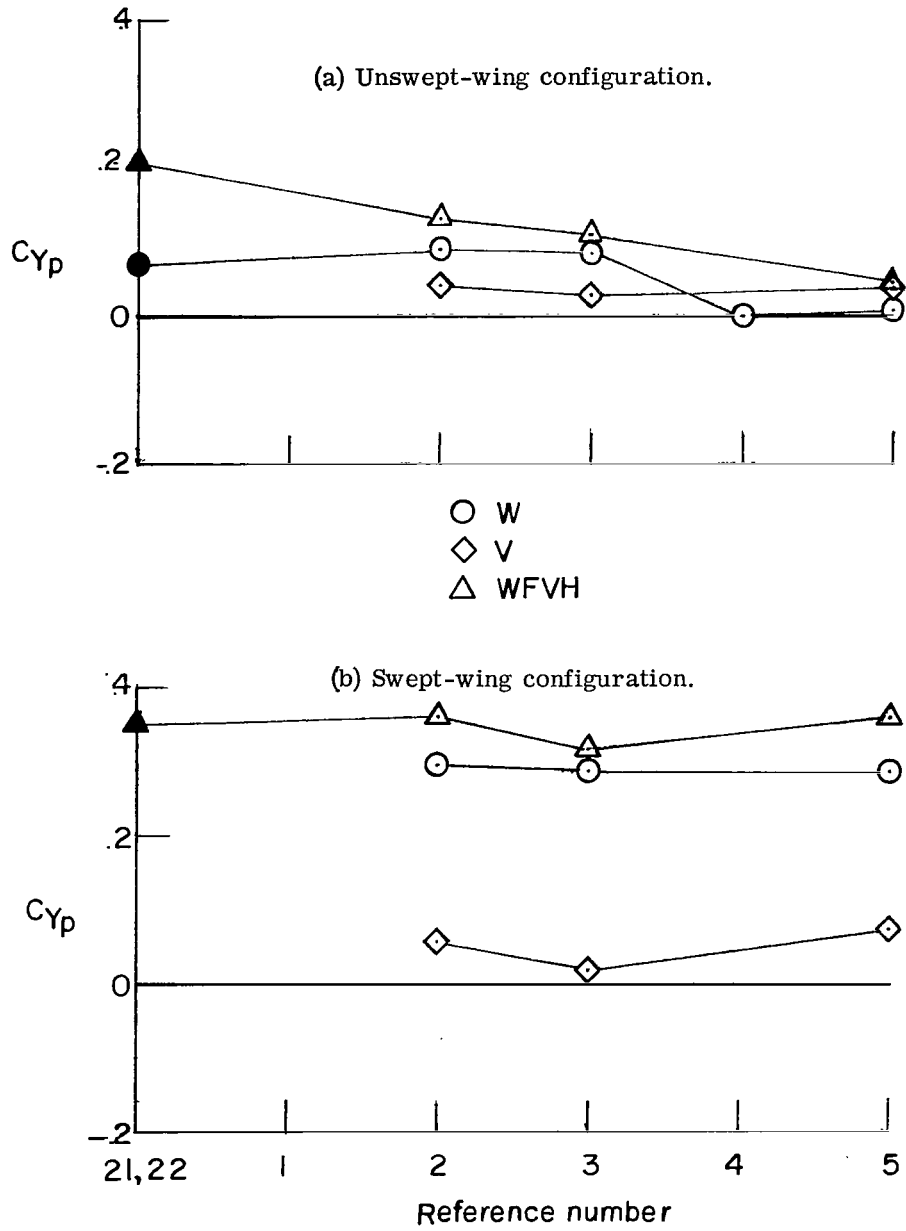


Figure 12.- Side force due to rolling velocity. Solid symbols indicate wind-tunnel data.

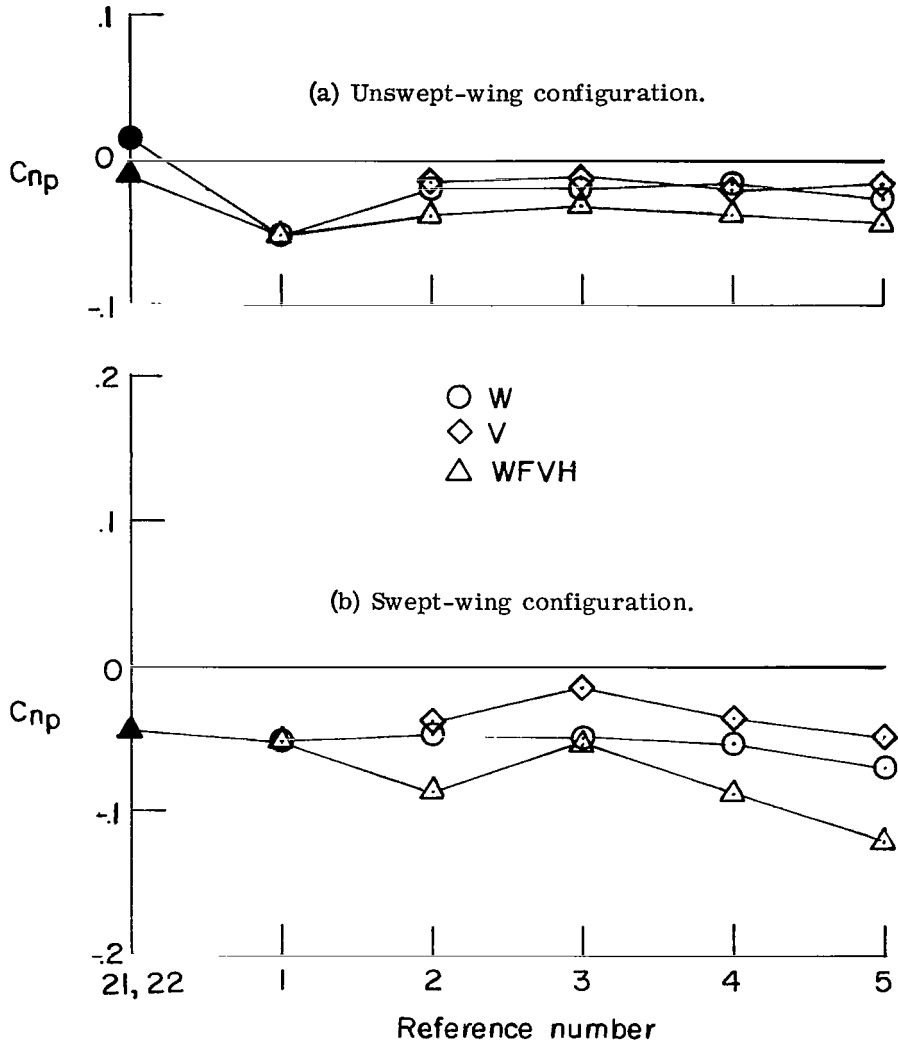


Figure 13.- Yawing moment due to rolling velocity or adverse-yaw parameter.  
 Solid symbols indicate wind-tunnel data.

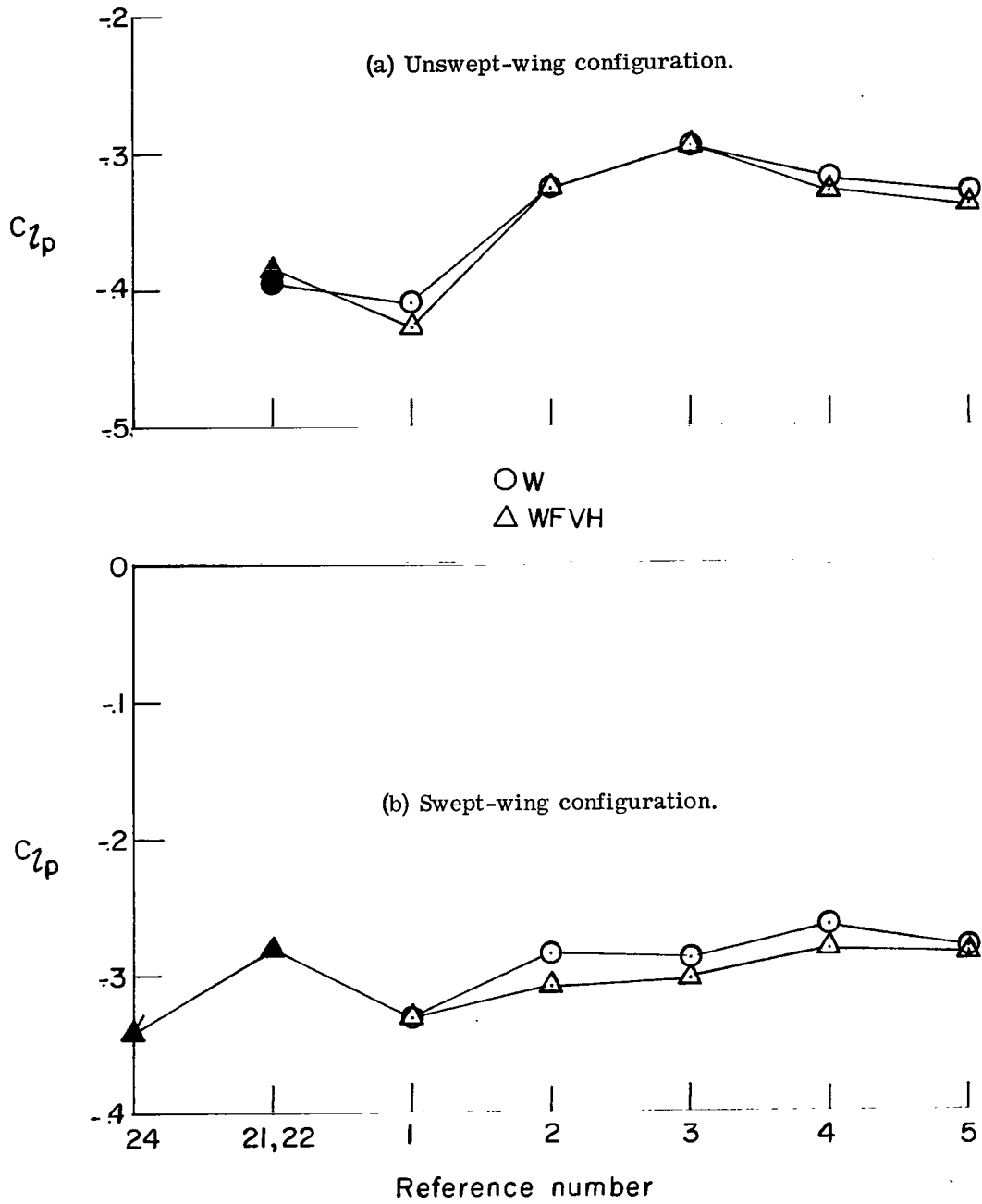


Figure 14.- Rolling moment due to rolling velocity or damping-in-roll parameter. Solid symbols indicate experimental data; flagged symbol indicates flight test.

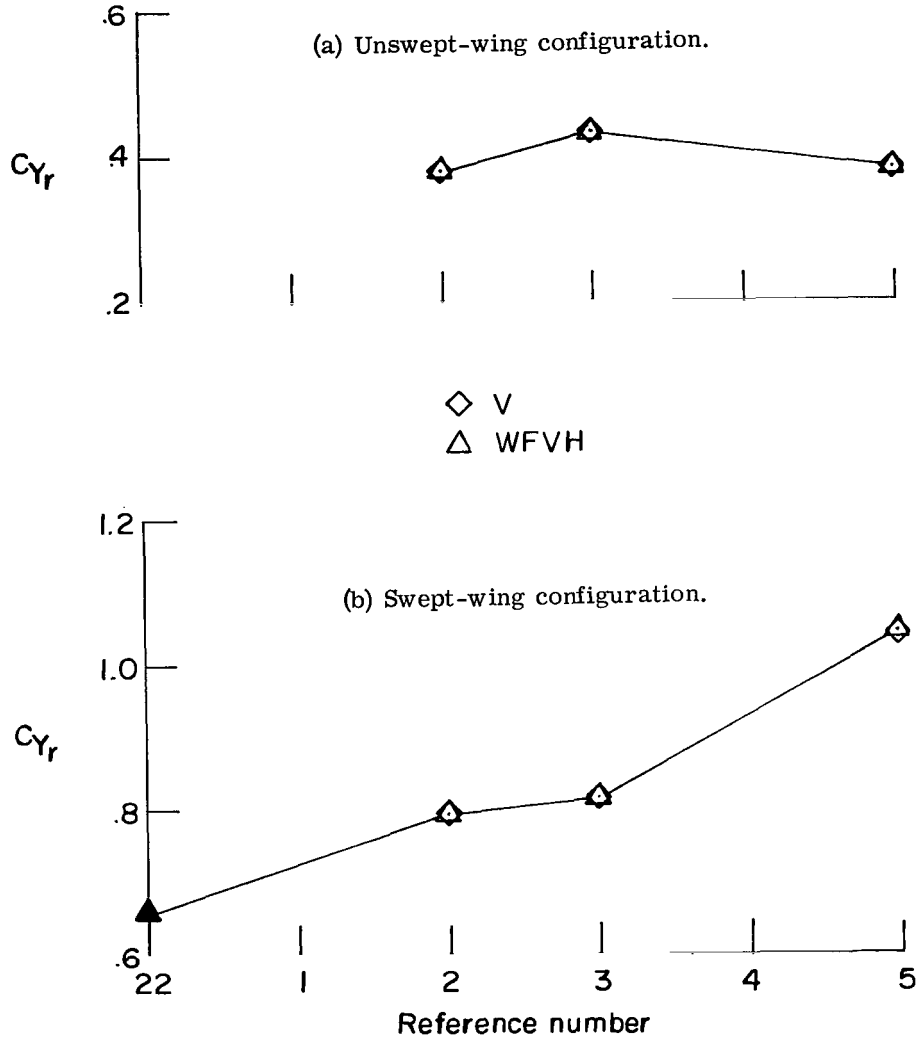


Figure 15.- Side force due to yawing velocity. Solid symbol indicates wind-tunnel data.

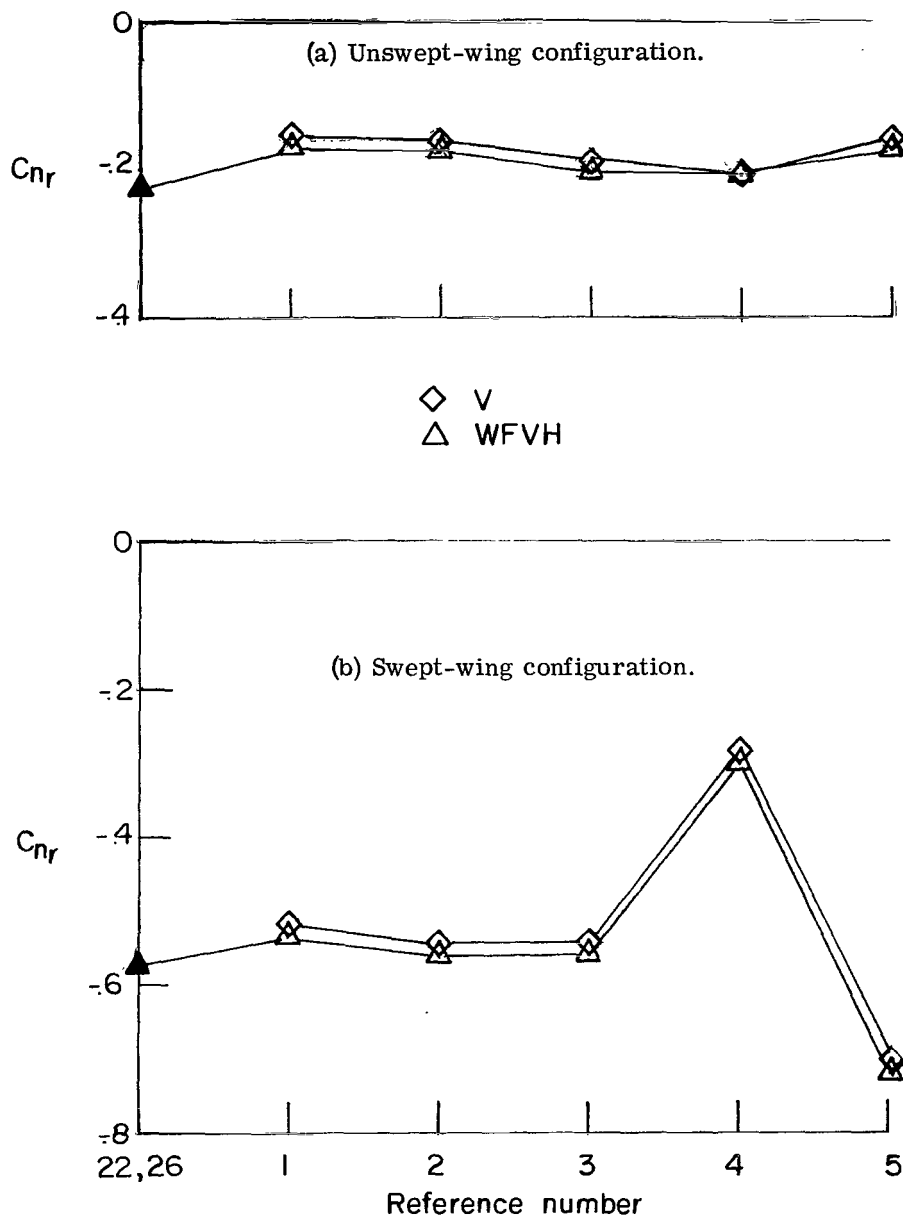


Figure 16.- Yawing moment due to yawing velocity or damping-in-yaw parameter.  
 Solid symbol indicates wind-tunnel data.

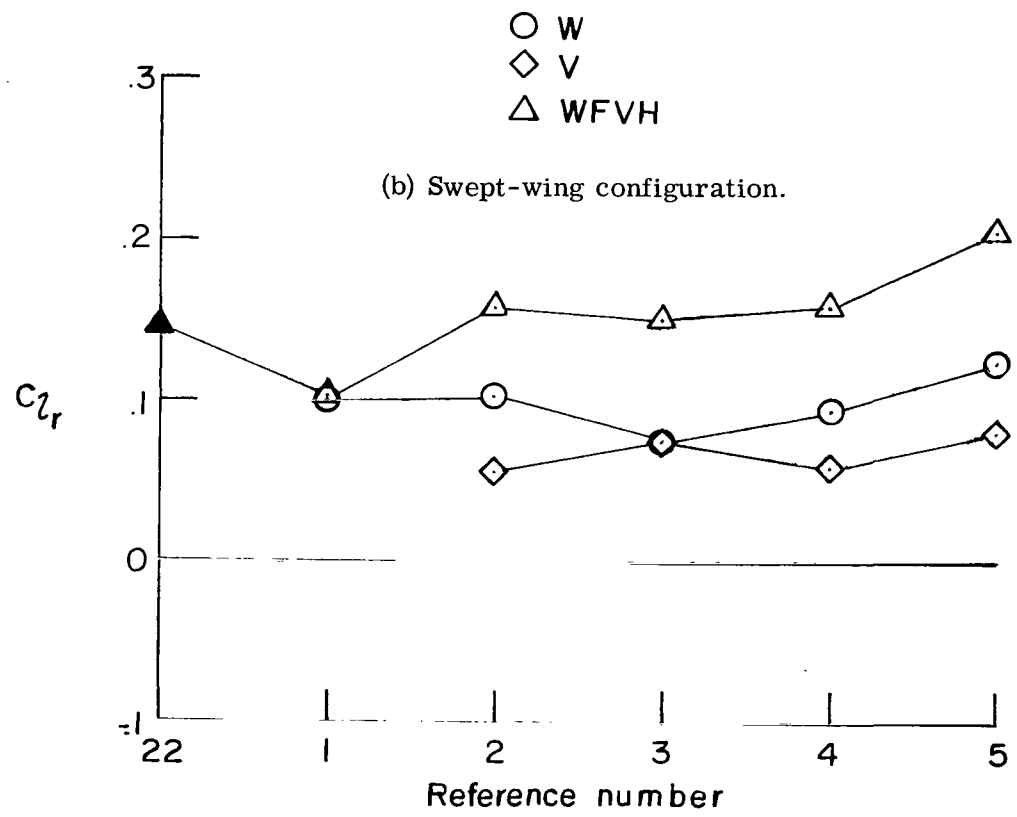
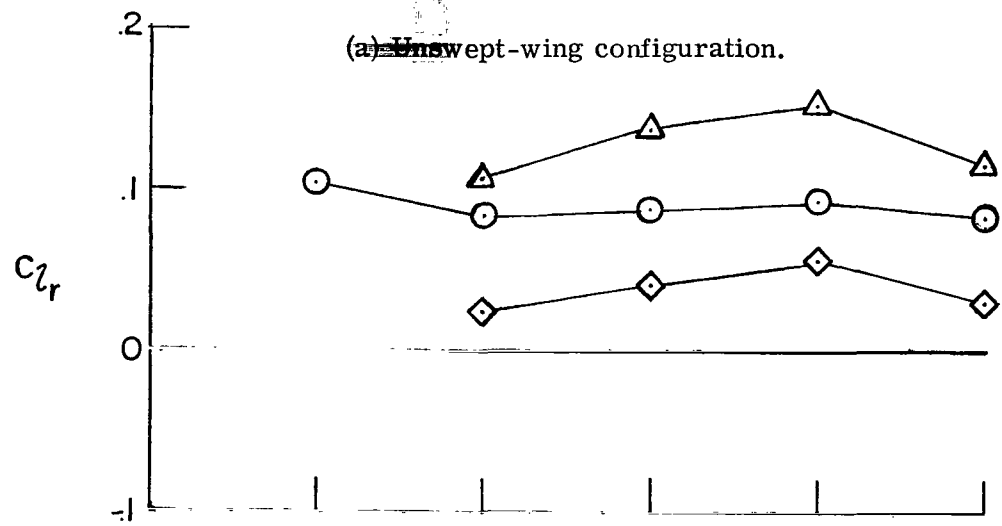


Figure 17.- Rolling moment due to yawing velocity. Solid symbol indicates wind-tunnel data.

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