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**Real Gas Effects on
Shock-Tube Performance at
High Shock Strengths**

by

J. L. Stollery

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Real gas effects on shock-tube performance
at high shock strengths

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J. L. Stollery*

SUMMARY

Calculations have been made to find the flow conditions behind shock waves in argon-free air of strengths $M_s = U/a_1$ up to about 35. The tables used are based on the currently accepted value for the dissociation energy of nitrogen of 9.758 e.v. per molecule, and are for equilibrium conditions.

Two cases only have been considered, namely:-

$$(i) \quad P_1 = \frac{1}{10} \text{ atm}, \quad T_1 = 290^\circ\text{K}$$

$$(ii) \quad P_1 = \frac{1}{100} \text{ atm}, \quad T_1 = 290^\circ\text{K}.$$

The driving conditions needed to produce such strong shocks have been calculated assuming "ideal" hydrogen ($\gamma = 1.41$) to be the driving gas.

In conclusion, the test conditions available through expanding the flow behind the shock are presented for an expansion ratio of 225 and the question of flight simulation is discussed.

* Department of Aeronautics, Imperial College. This work was done whilst acting as vacation consultant at R.A.E. during July-August 1957.

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1 Introduction

For shock strengths $M_s > 3$ real gas effects become increasingly important and for $M_s > 6$, perfect gas results are of little value. Calculations using real gas tables have been made by many authors, e.g. refs. 2, 3 (incorrect tables), 4, 5, 6 (corrected tables).

The corrected tables¹ permit calculation up to real gas temperatures of 15,000°K and Woods⁶ has used these to calculate the R.A.E. shock tube performance up to a real gas temperature T_2 of 8,000°K. In this note, the higher temperature conditions are examined. Any relaxation time effects have been neglected - i.e., the gas is assumed to be in the thermodynamic equilibrium and no attempt has been made to allow for shock attenuation.

2 Details of calculation*

Two sets of initial conditions were chosen:-

$$(i) P_1 = \frac{1}{10} \text{ atm} = 1.47 \text{ p.s.i.} \quad T_1 = 290^\circ\text{K}$$

$$\rho_1 = 0.000235 \text{ slugs/cu ft} \quad H_1 = 3.124 \times 10^6 \text{ ft lb/slug}$$

$$(ii) P_1 = \frac{1}{100} \text{ atm} = 0.147 \text{ p.s.i.} \quad T_1 = 290^\circ\text{K}$$

$$\rho_1 = 0.0000235 \text{ slugs/cu ft} \quad H_1 = 3.124 \times 10^6 \text{ ft lb/slug.}$$

2.1 Conditions behind the shock

Conditions behind a normal shock were found by a method similar to that given by Bird³. The main difference arose in the treatment of the equation

$$H_2 - H_1 = \frac{1}{2} (P_2 - P_1) \left(\frac{1}{\rho_2} + \frac{1}{\rho_1} \right)$$

to obtain ρ_2 . The presentation of the data in the new tables¹ made it more convenient to proceed as follows (than to follow the sequence described by Bird³):-

- (i) Given H_1 , P_1 and ρ_1 .
- (ii) Choose a value of T_2 .
- (iii) Plot $(H_2 - H_1)$ and $\frac{1}{2} (P_2 - P_1) \left(\frac{1}{\rho_2} + \frac{1}{\rho_1} \right)$ against ρ_2 from the tables¹. The point of intersection of the two curves gives ρ_2 .
- (iv) Read off the corresponding P_2 , H_2 and S_2 from the tables for the chosen T_2 .
- (v) Repeat the process for other values of T_2 .

* See list of symbols for definitions, page 11.

M_s and u_2 were found from

$$M_s^2 = \frac{P_2 - P_1}{a_1^2 \rho_1^2 \left(\frac{1}{\rho_1} - \frac{1}{\rho_2} \right)}$$

derived from the momentum and energy equations, and

$$u_2 = a_1 M_s \left(1 - \frac{\rho_1}{\rho_2} \right) \quad \text{continuity.}$$

The stagnation temperature and pressure (defined as those obtained by bringing the shock compressed air in region 2 isentropically to rest) were interpolated from the tables by calculating the stagnation enthalpy

$$H_{2_{st}} = H_2 + \frac{u_2^2}{2}$$

and moving along the isentrope S_2 until this value was reached.

These calculations enabled conditions behind the shock to be plotted against shock Mach number M_s and the results are shown in Figs. 1 to 8 inclusive.

2.2 Shock tube performance

The shock tube performance was calculated for each set of initial conditions assuming the driver gas to be ideal hydrogen ($\gamma_4 = 1.41$) at a pressure P_4 of 1000 atmospheres and various temperatures T_4 ranging from 290°K to 5,000°K. Again a graphical solution³ was employed. P_2 was plotted against u_2 from the previous calculations (section 2.1). P_3 was plotted against u_3 on the same graph, using the unsteady isentropic expansion relations

$$\frac{a_4}{a_3} = \left(\frac{P_4}{P_3} \right)^{\frac{\gamma_4 - 1}{2\gamma_4}} = 1 + \frac{\gamma_4 - 1}{2} M_3^2$$

(see for example ref.7). The point of intersection of the two curves gives the shock tube solution $P_2 = P_3$ and $u_2 = u_3$.

This enabled the shock strength that could be generated by each of two initial pressure ratios P_4/P_1 to be plotted against driver temperature (Fig.9). A cross plot of P_4/P_1 against M_s for a given T_4 is presented in Fig.10. The additional real air values were calculated at $M_3 = 1$ assuming that P_2/P_1 is independent of P_1 (see Fig.2).

2.3 Test conditions

The test section conditions in a non-reflected type of hypersonic shock tube with a nozzle expansion ratio of 225 were calculated assuming steady isentropic flow by solving the equations

$$\rho_2 u_2 A_2 = \rho_\infty u_\infty A_\infty \quad \text{where} \quad \frac{A_\infty}{A_2} = 225 \quad - \text{continuity} \quad (1)$$

$$H_2 + \frac{1}{2} u_2^2 = H_\infty + \frac{1}{2} u_\infty^2 = H_{2st} \quad - \text{energy} \quad (2)$$

$$S_2 = S_\infty \quad - \text{entropy} \quad (3)$$

Knowing all conditions 2, a T_∞ is selected so that ρ_∞ and H_∞ can be read off the tables at the given S . Velocity u_∞ is calculated from equation (2) and the product $\rho_\infty u_\infty$ is plotted against T_∞ . This is repeated for a range of T_∞ and the value satisfying equation (1) picked off. The corresponding u_∞ and Z_∞ are interpolated from tables whilst ρ_∞ is calculated from equation (1). P_∞ follows from $P = Z\rho RT$.

The test conditions were plotted to a base of M_s (Fig.11).

3 Results and discussion

3.1 Real gas effects on flow conditions behind the shock

The flow temperature T_2 falls far below the ideal value (Fig.1a) for shock strengths $M_s > 6$. This is due to the large increases in specific heat or heat capacity caused by

- (a) excitation of vibrational modes
- (b) dissociation
- (c) excitation of electrons
- (d) ionisation.

The approximate temperature bands in which dissociation and ionisation occur are marked on the figure. Thus the flow temperature in the region of the stagnation point of a missile travelling with twenty times the speed of sound at 100,000 ft will be around 7,500°K instead of 24,000°K predicted by perfect gas theory.

The corresponding stagnation temperatures in region 2 are presented in Fig.1b.

Fig.2 gives the pressure ratio P_2/P_1 across the shock, which closely follows the perfect gas law and is nearly independent of initial pressure P_1 . From the shock wave equations,

$$\frac{P_2}{P_1} = a_1^2 \frac{\rho_1}{P_1} \left(1 - \frac{\rho_1}{\rho_2} \right) M_s^2 + 1.$$

For strong shocks $\rho_2 \gg \rho_1$, so that $\frac{P_2}{P_1} \approx a_1^2 \frac{\rho_1}{P_1} M_s^2$, which for low temperatures T_1 becomes γM_s^2 (see Fig.2). Hence real gas effects are expected to be small.

The drop in temperature T_2 and only slight variation in pressure P_2 imply an increased density in the real gas which is shown as the

density ratio ρ_2/ρ_1 in Fig.3. The values are more than double the perfect gas estimates and the kinks correspond to dissociation and ionisation phenomena.

The velocity behind the shock, u_2 , is similar for real and perfect gases as expected from the continuity equation

$$u_2 = a_1 M_s \left(1 - \frac{\rho_1}{\rho_2}\right) \simeq a_1 M_s \quad \text{for large } M_s.$$

This approximate relation is also marked on Fig.4.

The real gas Mach number M_2 (Fig.5) rises to above 3 as compared with the perfect gas asymptote of 1.89 due to the reduced T_2 decreasing the speed of sound a_2 . The values of a_2 (not given in the tables) have been calculated using ref.4 where $a^2 = \gamma P/\rho$ and in that report γ

is defined as
$$\gamma = \left(\frac{\partial \log P}{\partial \log \rho}\right)_S.$$

The most striking real gas effect is on stagnation pressures assuming isentropic compression in the region behind the shock (Fig.6). For a shock Mach number of twenty, the real gas values are between ten and fifteen times the perfect values for the two cases considered. The reasons for the increase are (i) more energy is needed to produce a given M_s in real air than in a perfect gas - this can be seen from a comparison of the driving pressure ratios P_4/P_1 (Fig.10); (ii) the larger density ρ_2 in the real gas case. These large stagnation pressures give an indication of the reservoir conditions needed to generate high temperature flows.

In Fig.7, the stagnation pressure ratio P_{2st}/P_1 is plotted against stagnation temperature ratio T_{2st}/T_1 for both the single shock followed by steady isentropic compression, and steady isentropic flow. Curves for real and perfect gases are shown. The perfect gas relations are

$$\frac{P_{2st}}{P_1} \rightarrow \left(1 + \frac{1}{\gamma_1}\right)^{\frac{1}{\gamma_1-1}} \left(\frac{\gamma_1+1}{\gamma_1-1}\right) \frac{T_{2st}}{T_1} = 23 \frac{T_{2st}}{T_1} \quad \begin{array}{l} \text{shock compression case} \\ \text{for large } M_s, \text{ putting} \\ \gamma_1 = 1.4 \end{array}$$

and
$$\frac{P_{2st}}{P_1} = \left(\frac{T_{2st}}{T_1}\right)^{\frac{\gamma_1}{\gamma_1-1}} = \left(\frac{T_{2st}}{T_1}\right)^{3.5} \quad \begin{array}{l} \text{for steady isentropic} \\ \text{flow.} \end{array}$$

Comparing the real gas curves, shock compression to the same stagnation pressure P_{2st} gives around three times the stagnation temperature that would be achieved isentropically. Conversely for a given T_{2st} the stagnation pressure achieved is only one thousandth of that obtained by steady isentropic compression.

Finally in Fig.8 the Reynolds number per foot obtainable in region 2 is plotted versus M_s . The shape of the curve reflects the density changes since plots of both u_2 and μ_2 against M_s are sensibly smooth. The theoretical values for viscosity are taken from "Thermodynamics and Physics of Matter" by Rossini, p.374 Table D.6.b., and do not allow for the effects of dissociation.

3.2 Shock tube performance

The shock strengths that can be generated by perfect dry hydrogen at 1000 atmospheres and various temperatures are shown in Figs. 9 and 10 and compared with the perfect gas solutions⁷

$$\frac{P_4}{P_1} = \frac{P_2}{P_1} \cdot \frac{P_4}{P_3} = \left\{ \frac{2\gamma_1}{\gamma_1+1} M_s^2 - \frac{\gamma_1-1}{\gamma_1+1} \right\} \left\{ 1 - \frac{a_1}{a_4} \left(\frac{\gamma_4-1}{\gamma_1+1} \right) \left(M_s - \frac{1}{M_s} \right) \right\}^{\frac{-2\gamma_4}{\gamma_4-1}}$$

The benefit of heating the driver gas is marked; at pressure ratios above 10^3 the shock Mach number is roughly doubled by heating the hydrogen to 2000°K. For example, with dry hydrogen at $P_4 = 1000$ atm and $T_4 = 2000^\circ\text{K}$, shock strengths rising to $M_s = 26$ are possible in real air as the initial pressure P_1 is reduced to 10^{-2} atm.

Such a temperature can be attained by constant volume combustion of a hydrogen-oxygen mixture, but this results in a wet driver gas of increased molecular weight. The speed of sound a_4 is thus reduced and this reduction decreases M_s by comparison with the values shown on Fig.10. These effects are more fully discussed in ref.6.

Heating by electrical discharge is also a possibility though there is little data on the behaviour of arcs at high pressures in hydrogen⁸.

3.3 Conditions after expansion

The working section conditions with a nozzle of area ratio 225 are presented in Fig.11. Although the test density, pressure and velocity are representative of high altitude hypersonic flight, the flow temperature and hence Mach number are not. This result is obvious from Fig.7, which shows how entirely different are the pressure-temperature relations for shock compression and isentropic expansion. With the low channel

pressures $\left(P_1 = \frac{1}{10} \text{ and } \frac{1}{100} \text{ atm} \right)$ considered here, there are two possible sets of test conditions:

- (i) correct pressures, but high flow temperatures;
- (ii) correct temperatures, but very low pressures.

The second alternative requires extremely large nozzle expansion ratios and it will be difficult to avoid slip flow. The remedy is to use higher values of P_1 or ideally, compression and expansion processes having similar pressure temperature relations. The conclusion is that for the conditions considered here, complete simulation is only possible at extreme altitudes.

4 Flight simulation at hypersonic speeds

Consider hypersonic flight at 90,000 ft. The relevant atmospheric data¹⁴ are $P = 0.017$ atm, $T = 218^\circ\text{K}$, $\rho = 5.44 \times 10^{-5}$ slugs/cu ft and no dissociation or ionisation. Obviously, if a full scale model of all or part of a vehicle can be tested in a stream of undissociated air with the above flow conditions and at the correct velocity, then simulation is complete (the model would have to be preheated if equilibrium temperature conditions are needed, since the testing time is so short). Limiting the discussion to shock compression and isentropic expansion of real air the following table can be compiled:-

| TEST MACH NO. M_∞ | | | 5 | 10 | 15 | 20 |
|--------------------------|---------------------------------------|---|---------|---------|-----------------|-----------------|
| (1) | $(1 + 2M_\infty^2) 218^\circ\text{K}$ | Perfect gas stagnation temp. | 1,310 | 4,580 | 10,000 | 17,600 |
| (2) | T_{2st} | Real gas stagnation temp. from Fig.1b - extrapolating for $P_1 = 1$ atm | 1,310 | 4,300 | 6,700 | 9,500 |
| (3) | M_S | Read off Fig.1b using row (1) | 3.2 | 6.8 | 9.8 | 13 |
| (4) | $\frac{T_{2st}}{T_1}$ | $T_1 = 290^\circ\text{K}$ | 4.5 | 14.8 | 23.1 | 32.8 |
| (5) | $\frac{P_{2st}}{P_1}$ | From the shock compression curve of Fig.7. Extrapolate for $P_1 = 1$ atm | 53 | 600 | 2,000 | 4,000 |
| (6) | $\frac{P_{2st}}{P_\infty}$ | From steady isentropic flow curve of Fig.7. Extrapolate for $P_1 = 1$ atm | 250 | 10^5 | of order 10^6 | of order 10^7 |
| (7) | P_1 required | $= \frac{(6)}{(5)} \times 0.017$ atm | 0.8 atm | 2.8 atm | of order 10 atm | of order 50 atm |
| (8) | P_4 required | From Fig.10 assuming $T_4 = 2,000^\circ\text{K}$ | 16 atm | 400 atm | 4,500 atm | 70,000 atm |
| (9) | Expansion ratio | Taken from ref.2 approx, only | 40 | 1,000 | 20,000 | 300,000 |

Strictly, the values for $M_\infty = 10, 15$ and 20 need iteration for the correct P_1 but the object is merely to indicate orders of magnitude. A similar calculation for simulation at an altitude of 180,000 ft showed a reduction of P_1 and P_4 by a factor 10. From these figures, it is obvious that if complete simulation at the higher Mach numbers is required then

- (i) the channel must be pressurised;
- (ii) driving pressures will be very large;
- (iii) extremely big expansions will be needed so that the testing of fairly large models is possible.

4.1 Blunt bodies

For some investigations, Mach number is an unimportant parameter. Kurzweg and Wilson⁹ show that for blunt bodies, the local Mach numbers around a major part of the nose region are independent of flight Mach numbers above 5. The important quantities are local density and temperature. Fig.12 shows the real and simulated conditions. If the relaxation distance is small compared with the stand off distance then the gases in both cases will be in thermal equilibrium and of similar chemistry. In particular at the stagnation point both M and Re are of less importance than the flow chemistry. Fay and Riddell¹⁰ show that for a stagnation point boundary layer in thermal equilibrium the important quantities are stagnation enthalpy and density. These can readily be simulated in the shock tube without expanding the flow. If, however, the layer has not reached equilibrium, there can be scale effects which make complete simulation more difficult.

4.2 Slender bodies

Slender body results should theoretically correlate on the parameter $(M^3 \sqrt{C}) / \sqrt{Re_x}$ if the leading edge is sharp, but the experimental work of Bogdonoff and Hammitt¹¹ and the more recent theory of Lees¹², have shown the extreme importance of the leading edge. In reality no edge is sharp and the body pressures seem to depend on the leading edge thickness and shock wave shape. It is possible to simulate conditions at the edge correctly and the shock wave shape alters very little at $M_\infty > 10$.

Moreover a considerable portion of the mass that enters the boundary layer has crossed a near normal detached shock at the leading edge and so may have the correct flow properties. What will certainly be wrong is the transverse temperature gradient between the edges of the boundary layer and the shock wave at stations well downstream from the nose, unless M_∞ is correctly simulated.

The various ways of using a shock tunnel showing simulated conditions and the corresponding difficulties are tabulated below.

The flow characteristics are

| P, | P_{st} , | ρ , | ρ_{st} , | T, | T_{st} , | u, | M, | Re, | H |
|----|------------|----------|---------------|----|------------|----|----|-----|----|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |

/Table

| Type of Tube | Initial Conditions | Quantities Simulated | Difficulties |
|--|---|--|--|
| Basic tube plus large expansion to the correct M_∞ | $P_1 > 1 \text{ atm}$ | 1-10 incl. | Lengthy nozzle; long starting time; very high P_4 |
| Basic tube | Adjust for desired $4 + 10$ | 2,4,6,7,9,10. Flow at the stagnation point | Small model - could use a small expansion to avoid this |
| Basic tube plus expansion to $M_\infty = 5$ | Vary P_1 for range of 9 | 2,4,6,7,9,10. Flow around the nose of blunt bodies | |
| Basic tube plus expansion to $M_\infty = 10$ or to correct value | Low M_s \therefore low $\frac{P_4}{P_1}$ | 1,3,8,9. No real gas effects | Dry air, operate just above air liquefaction temperature |

5 Conclusions

- (i) For the conditions considered in this report the real gas effects on pressure and velocity behind the shock are small.
- (ii) The real gas effects on density, temperature, Mach number and particularly on stagnation pressure, are marked.
- (iii) For a hydrogen-driving-air shock tube the shock strength M_s is reduced by 5-10% at a given pressure ratio P_4/P_1 due to real gas effects.
- (iv) There is a marked increase in the shock strength if the driver gas is heated.
- (v) Complete simulation of flight conditions in a shock tunnel is very difficult, basically because of the dissimilar compression and expansion cycles used to generate the flow, and a pressurised channel will usually be needed. Complete simulation of the flow near the stagnation point is however much simpler.

Acknowledgment

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LIST OF SYMBOLS

| | |
|----------|--|
| P | pressure |
| ρ | density |
| T | temperature |
| R | gas constant |
| u | flow velocity |
| U | shock velocity |
| S | specific entropy |
| H | specific enthalpy |
| γ | ratio of specific heats |
| a | local speed of sound |
| M | Mach number |
| Re | Reynolds number |
| C | constant in viscosity-temperature relation $\frac{\mu}{\mu_{\infty}} = C \frac{T}{T_{\infty}}$ |
| μ | viscosity |
| Z | compressibility factor ($= 1 + \alpha$ where α is the fraction of the original number of molecules that has dissociated) |
| A | area |

Subscripts

| | |
|----------|--|
| 1 | Conditions in front of shock wave |
| 2 | Conditions behind shock wave |
| 3 | Conditions behind interface |
| 4 | Conditions behind rarefaction fan, i.e. initial high pressure chamber conditions |
| s | shock wave |
| st | stagnation conditions |
| ∞ | test conditions |
| x | distance from the leading edge |

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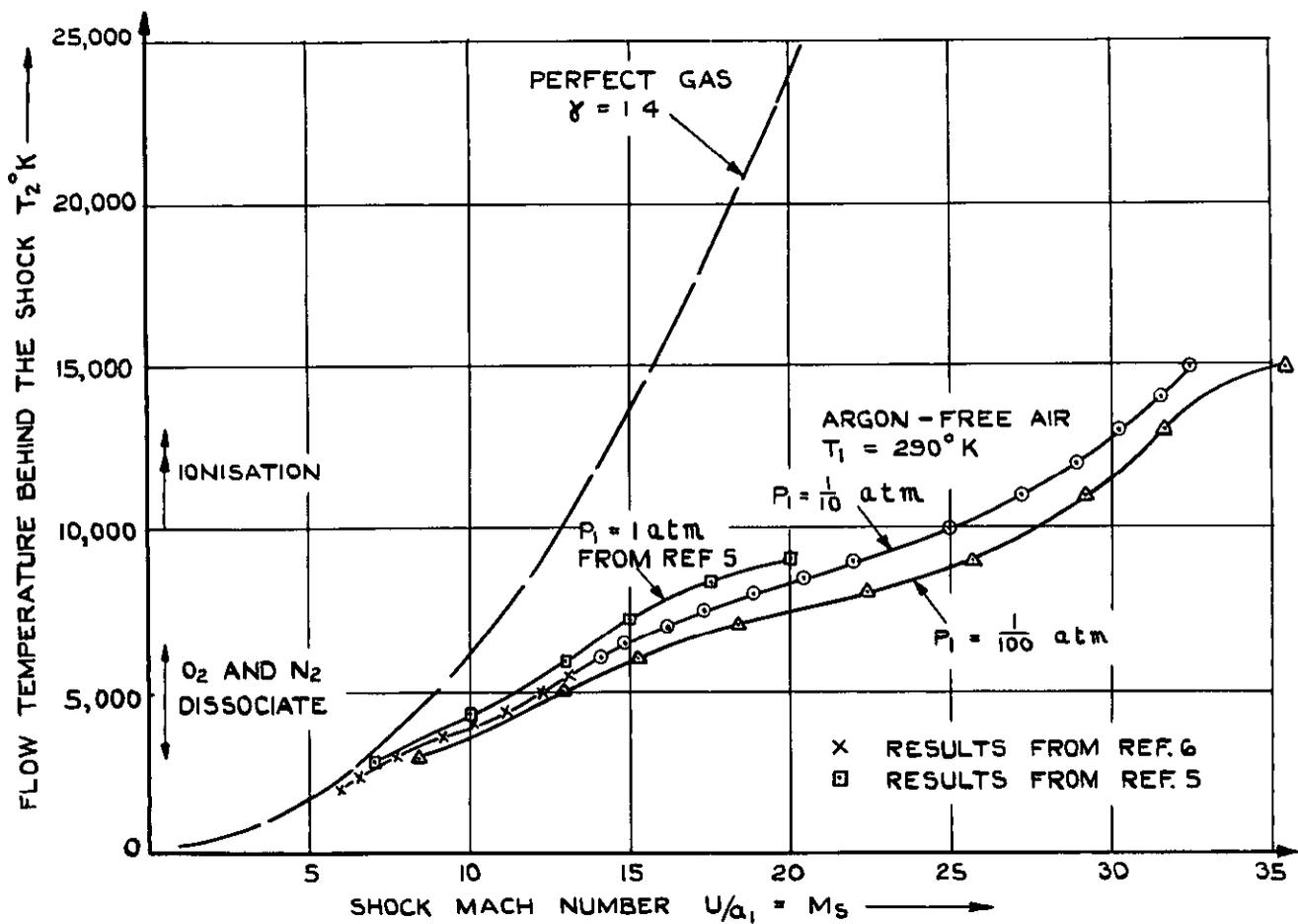


FIG. 1.(a) FLOW TEMPERATURES.

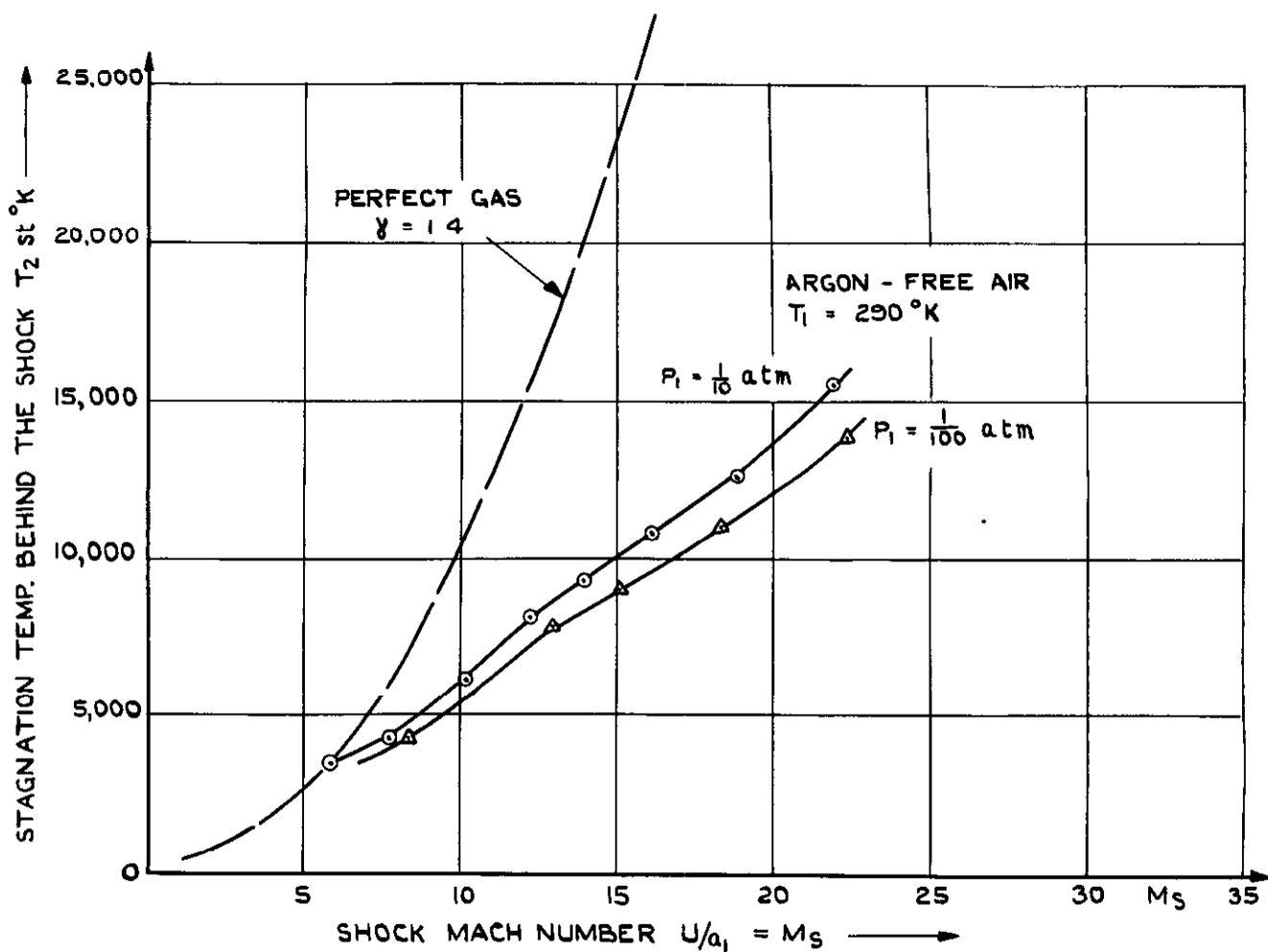


FIG. 1.(b) STAGNATION TEMPERATURES.

- X \odot $P_1 = \frac{1}{10}$ atm. (X ARE FROM REF. 6.)
- Δ $P_1 = \frac{1}{100}$ atm
- APPROX. RELATION $\frac{P_2}{P_1} = \gamma M_s^2$.
- \square $P_1 = 1\pi$ FROM REF. 5.

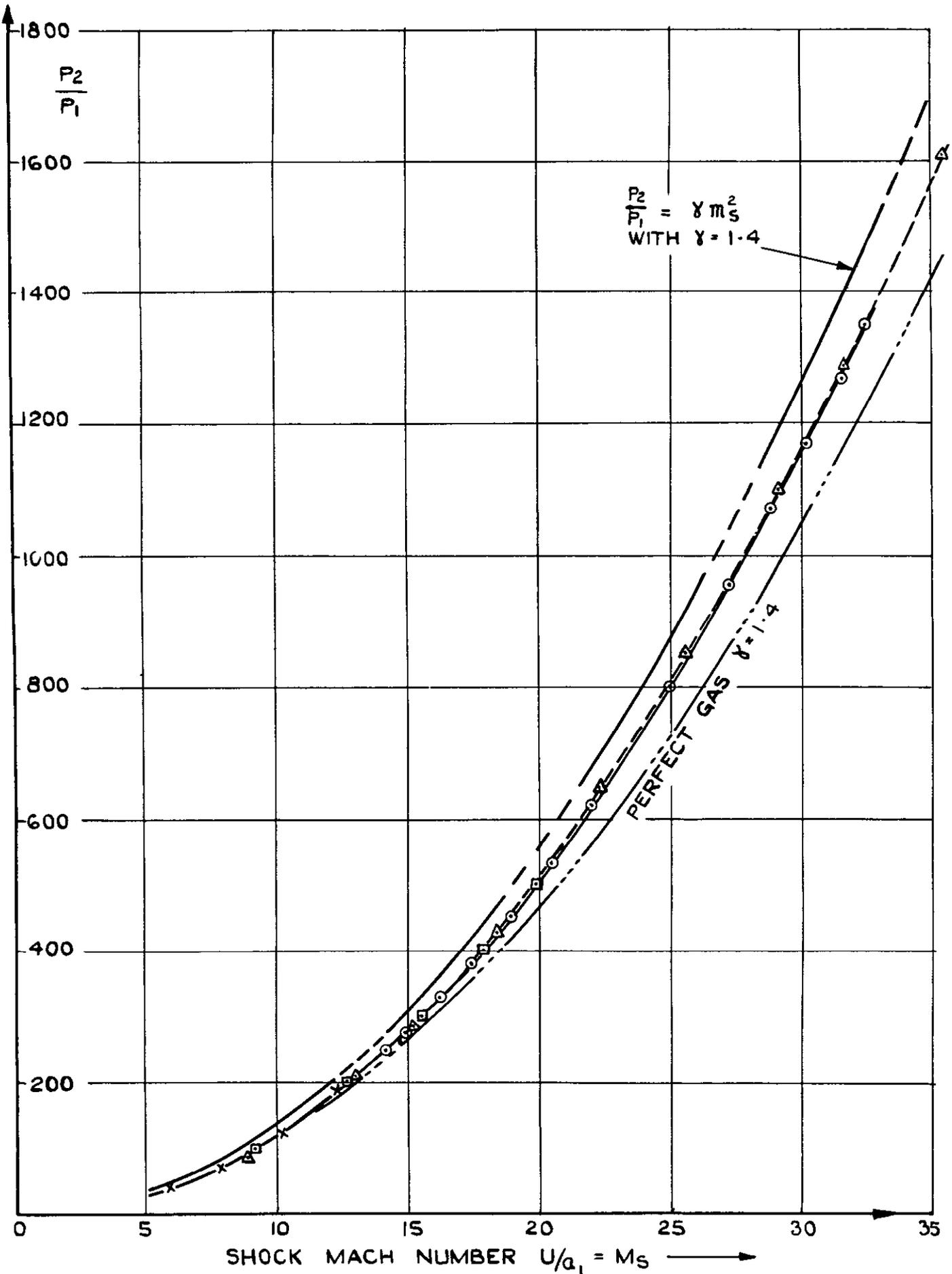


FIG. 2. PRESSURE RATIO ACROSS THE SHOCK.

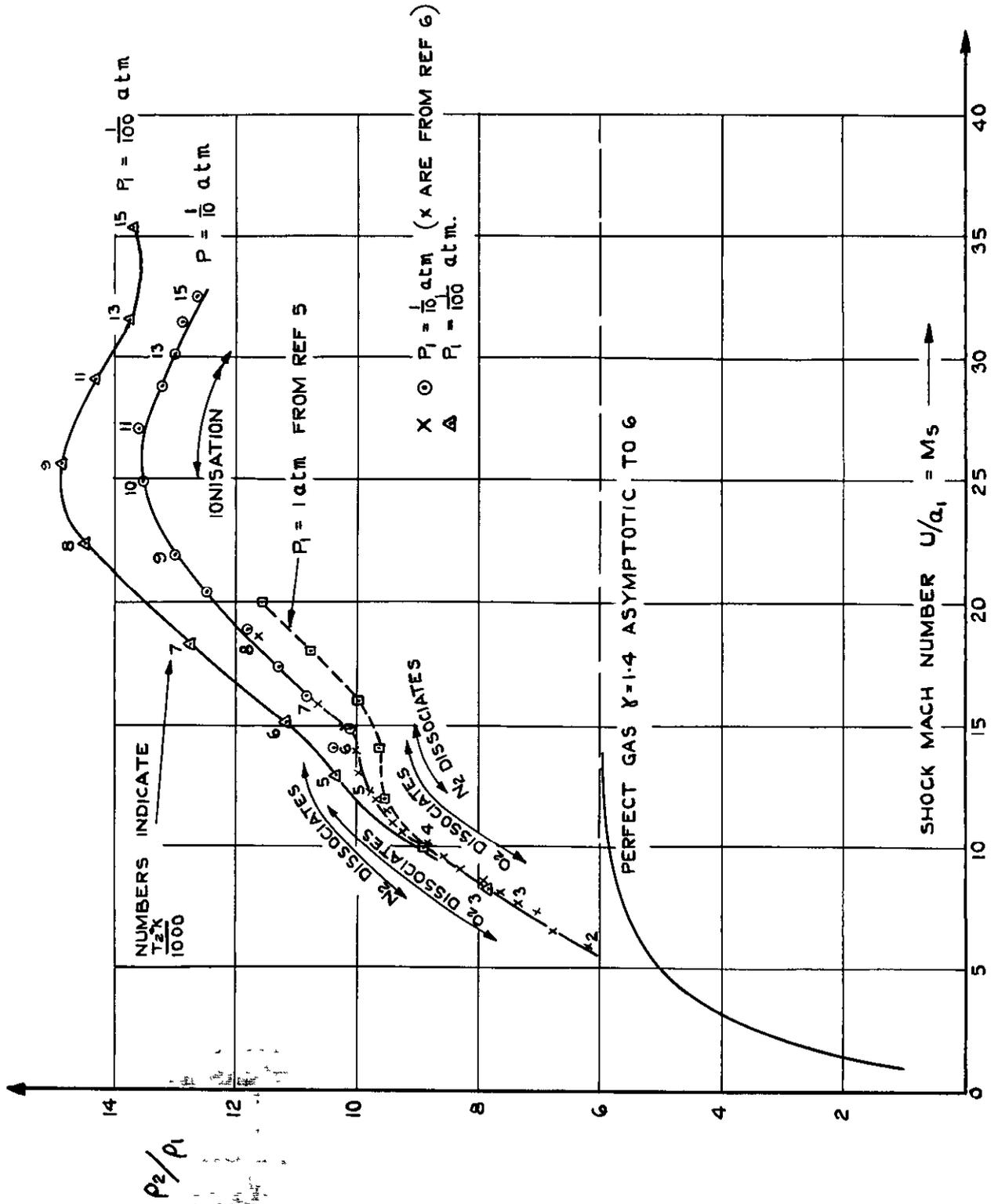


FIG. 3. DENSITY RATIO ACROSS THE SHOCK.

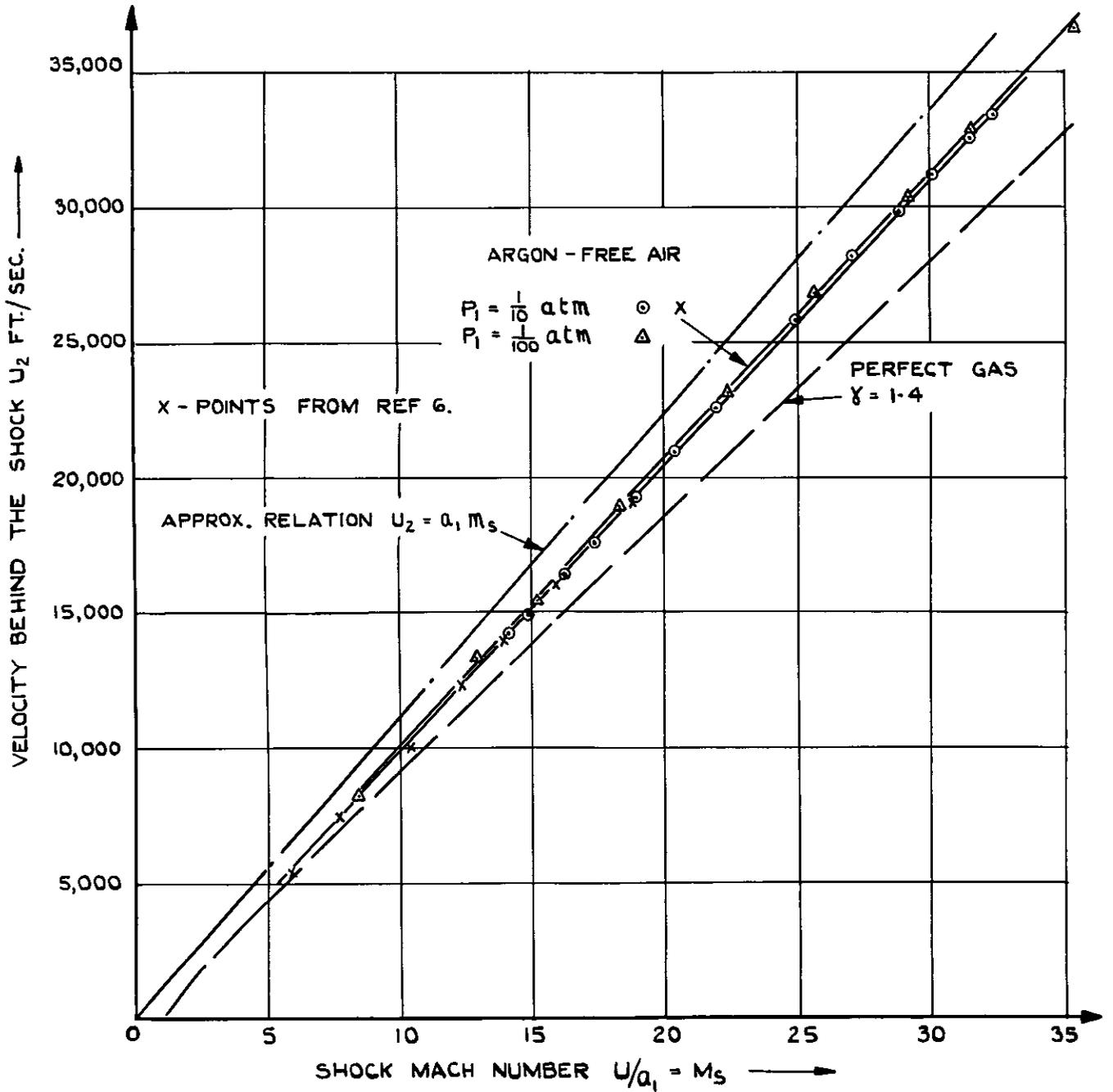


FIG. 4. VELOCITY BEHIND THE SHOCK.

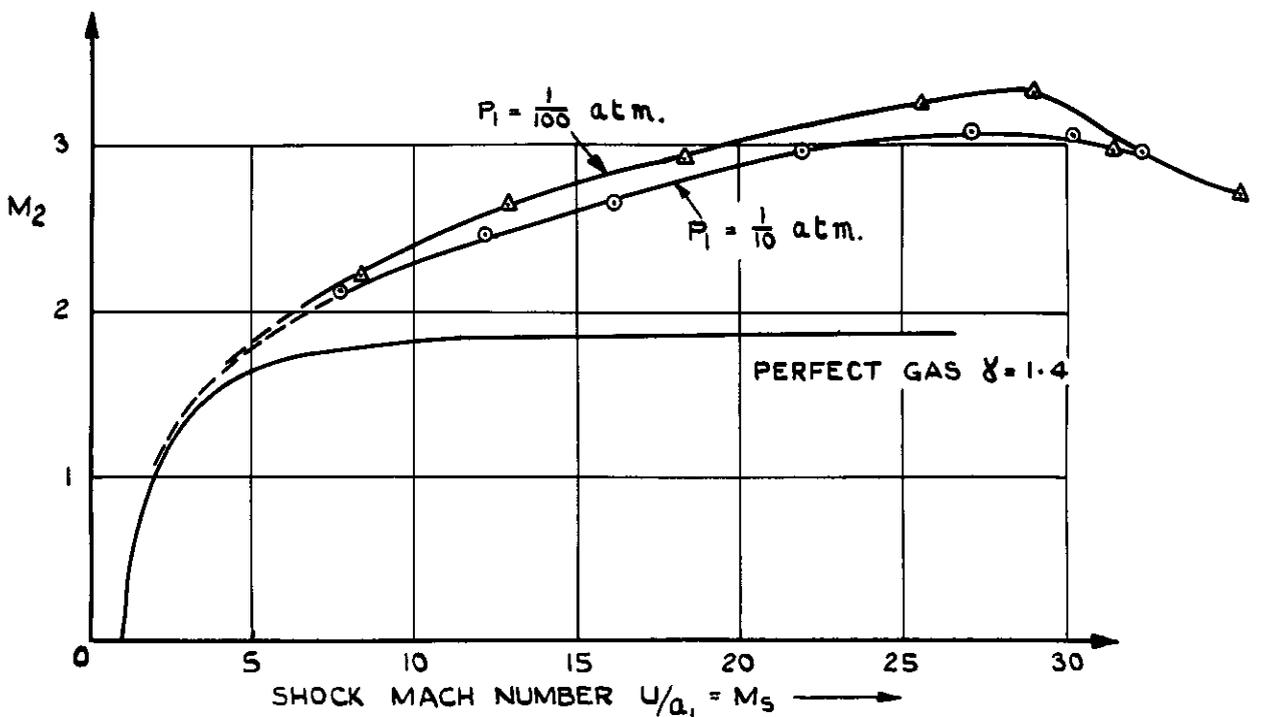


FIG. 5. MACH NUMBER BEHIND THE SHOCK.

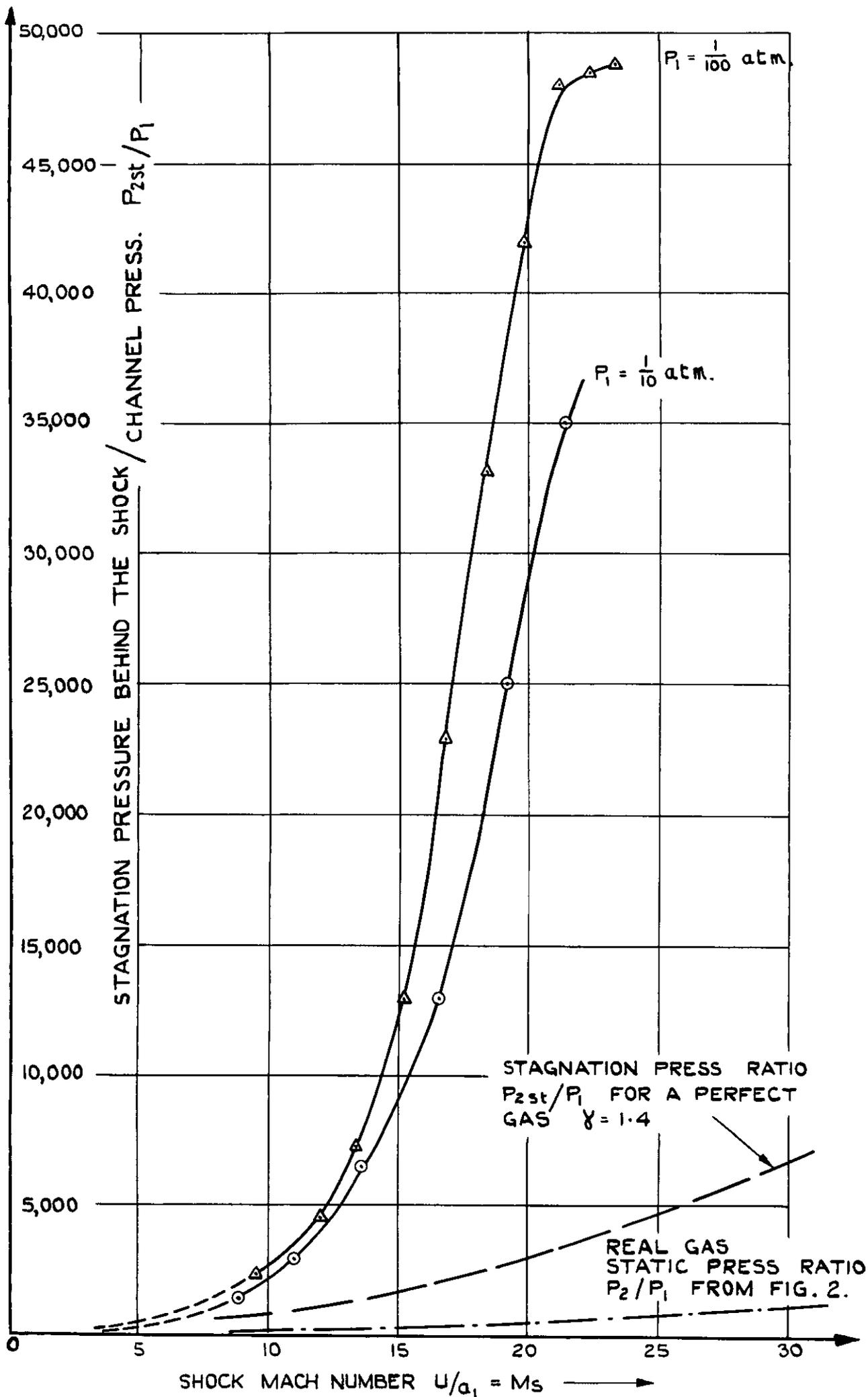


FIG. 6. STAGNATION PRESSURE BEHIND THE SHOCK.

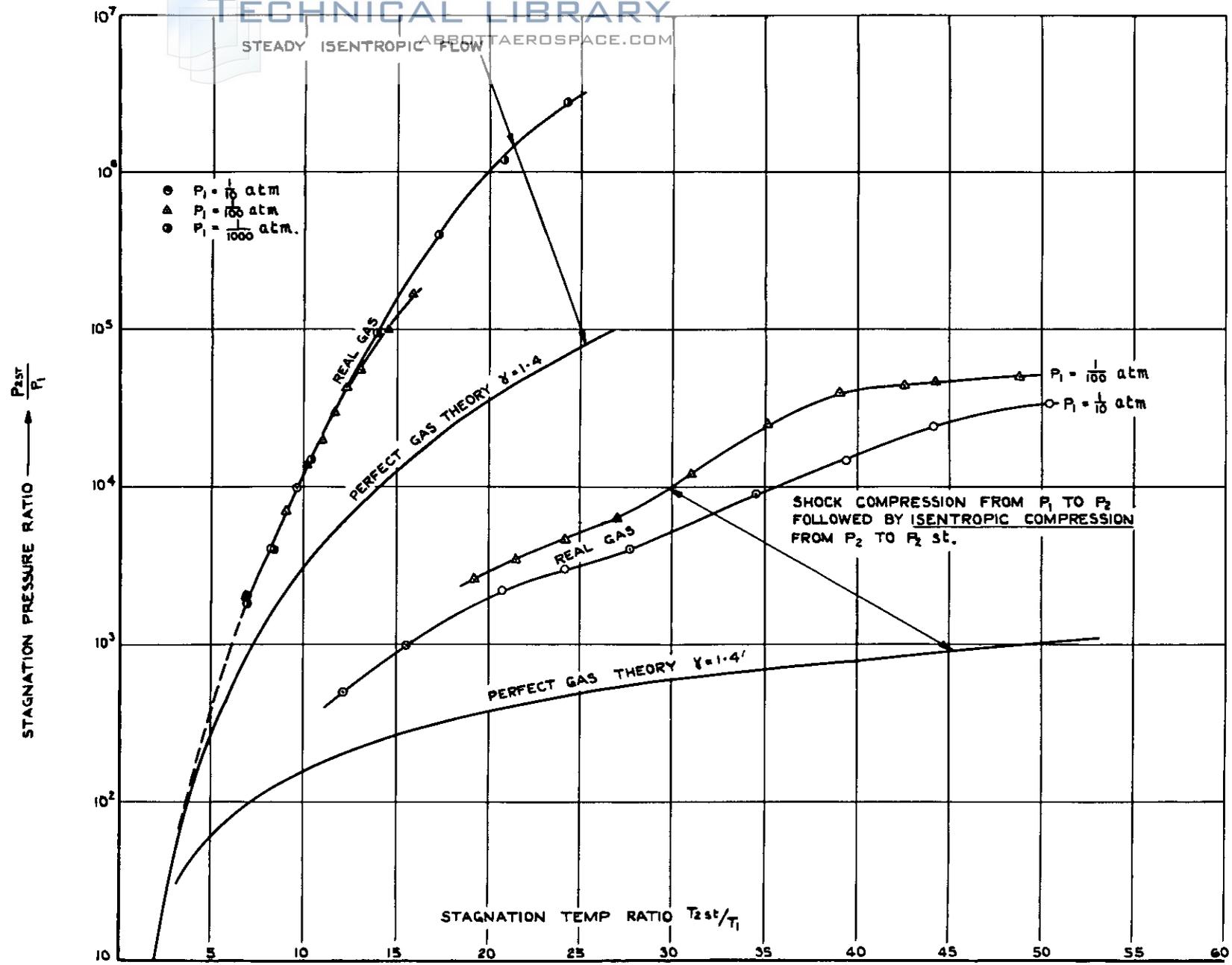


FIG. 7. STAGNATION CONDITIONS.

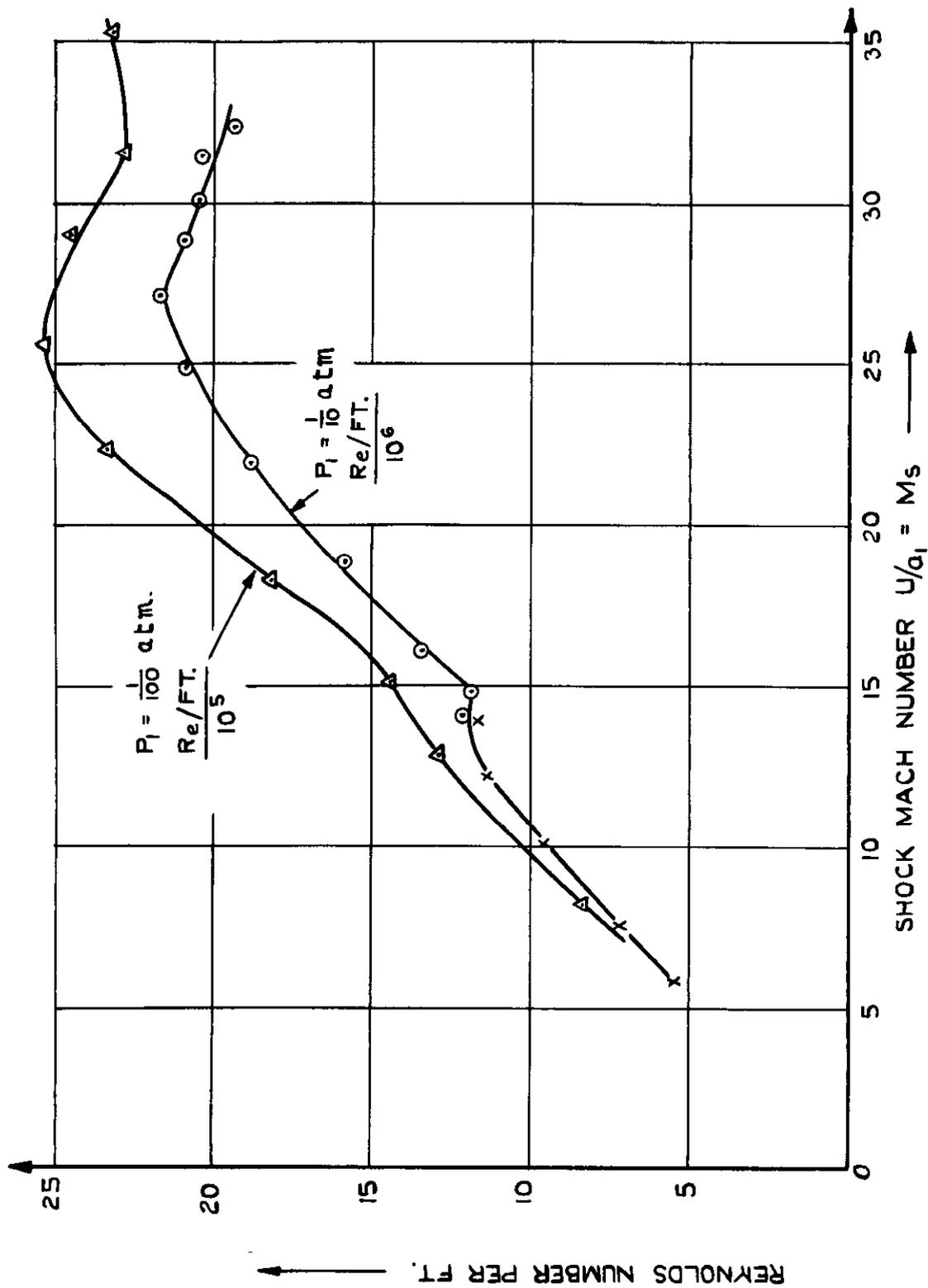


FIG. 8. REYNOLDS NUMBER PER FOOT BEHIND THE SHOCK.

DRIVER GAS IS PERFECT DRY H₂ ($\gamma = 1.41$) AT $P_4 = 1000$ ATM.

DRIVEN GAS IS REAL ARGON-FREE AIR AT $T_1 = 290^\circ\text{K}$ AND VARIOUS P_1

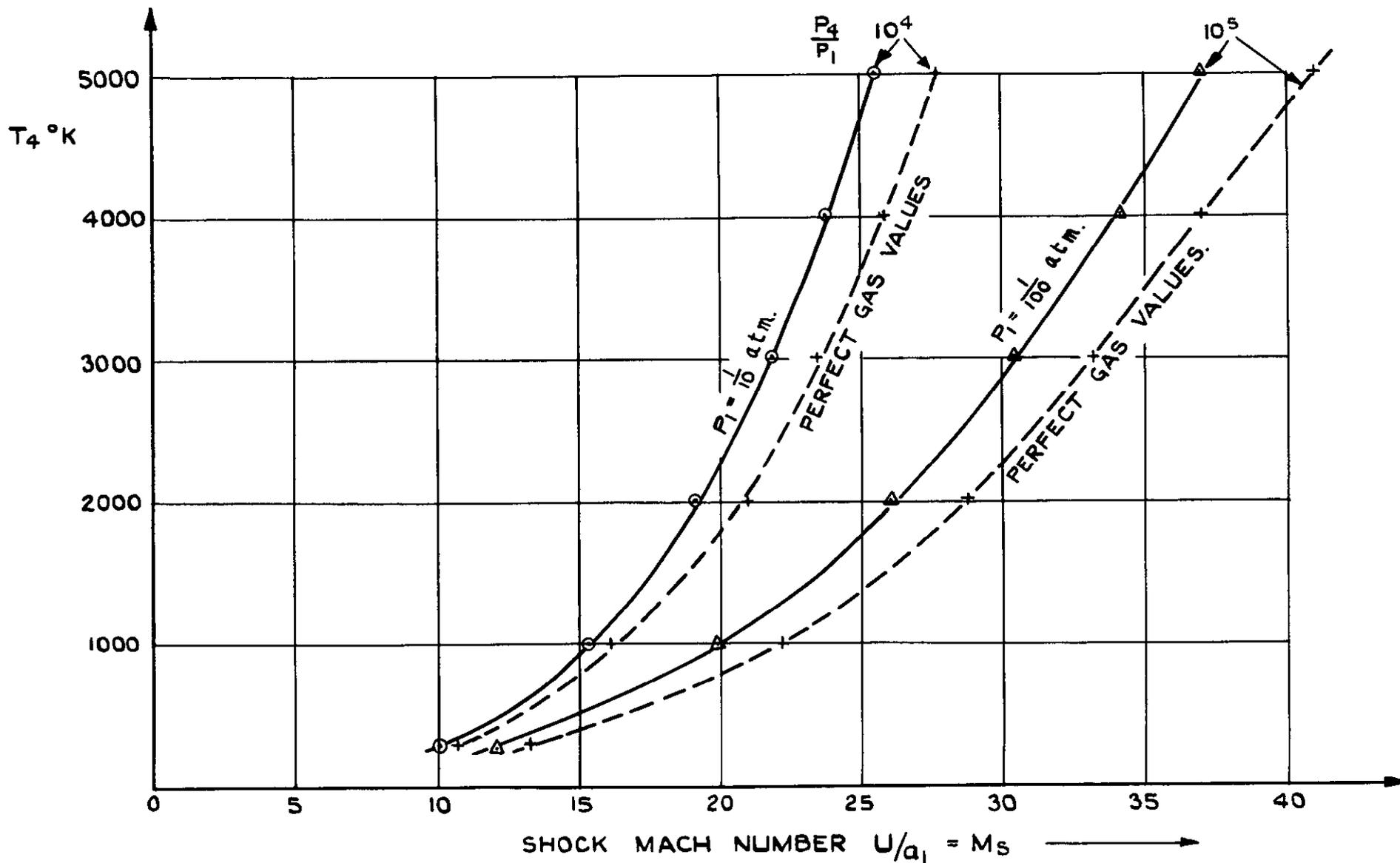


FIG. 9. EFFECTS OF HEATING THE DRIVER GAS.

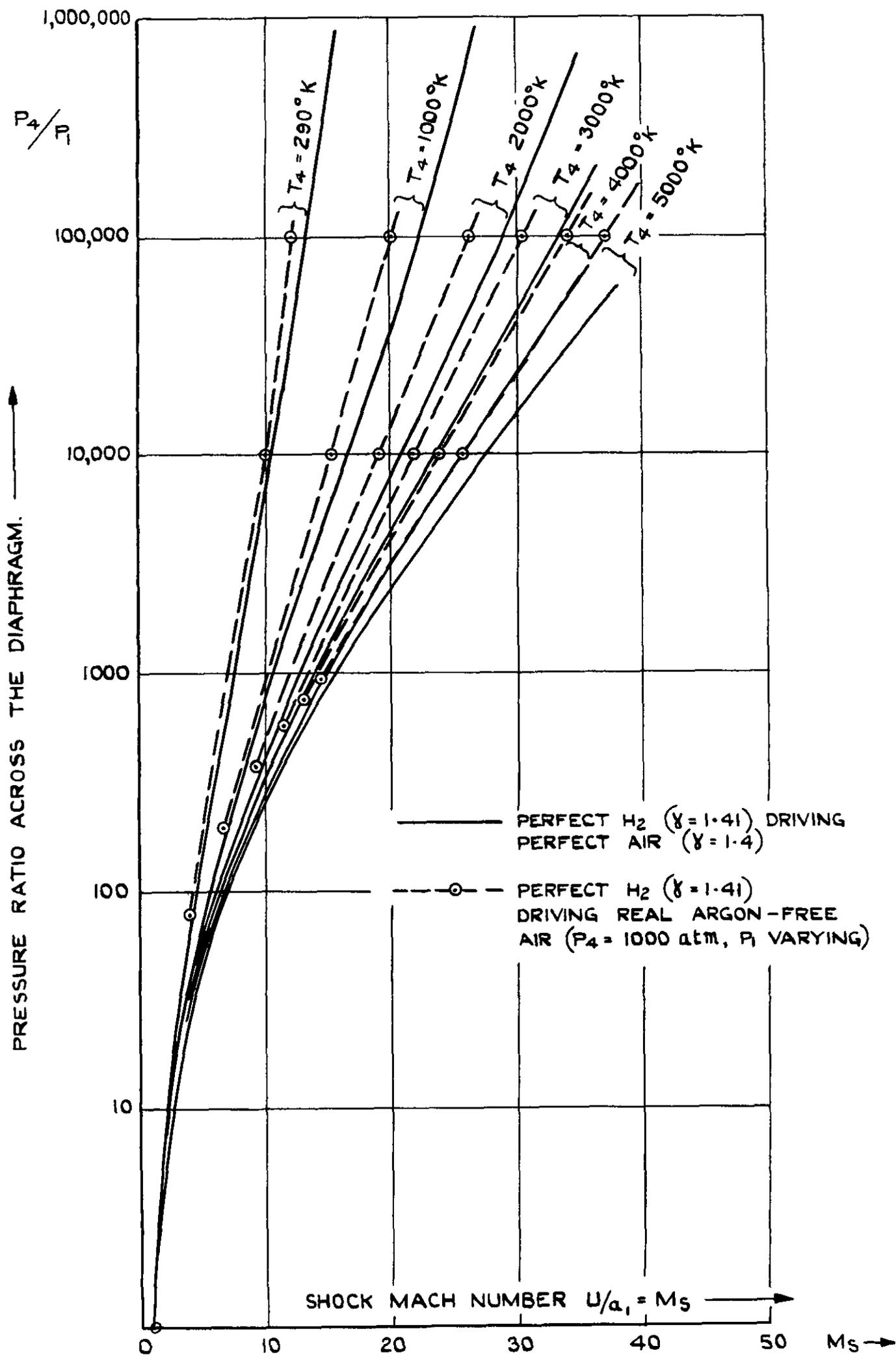


FIG. 10. SHOCK-TUBE PERFORMANCE.

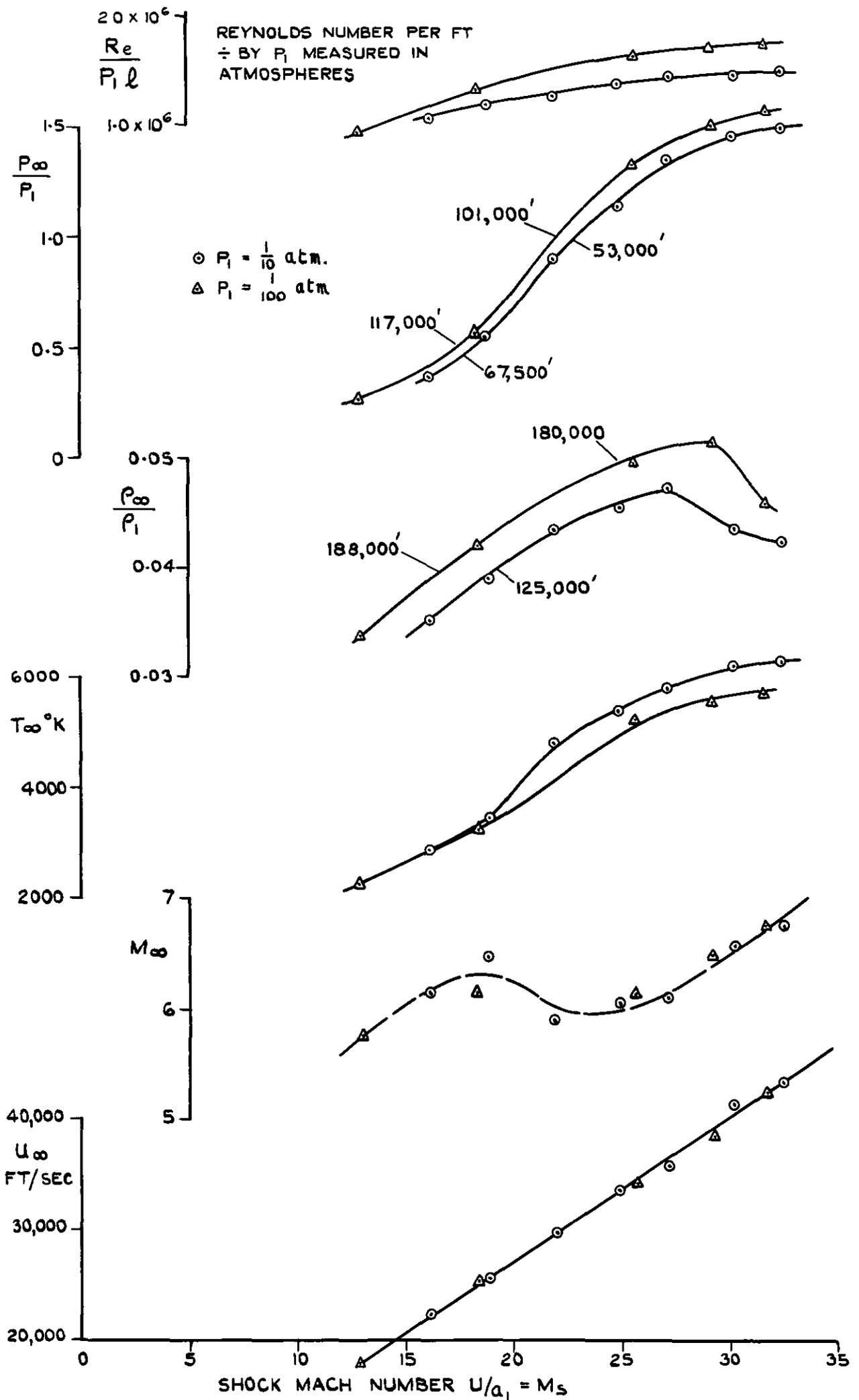
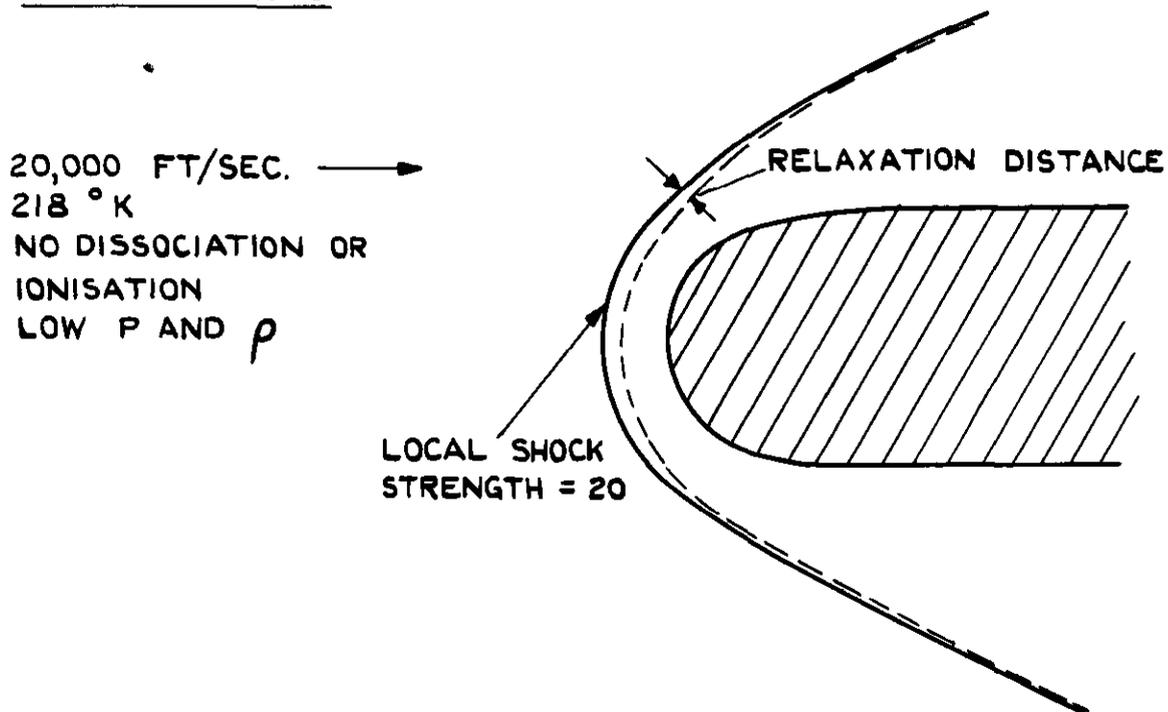


FIG. II. FLOW CONDITIONS AFTER AN EXPANSION RATIO OF 225.

REAL CONDITIONS.



SIMULATED CONDITIONS.

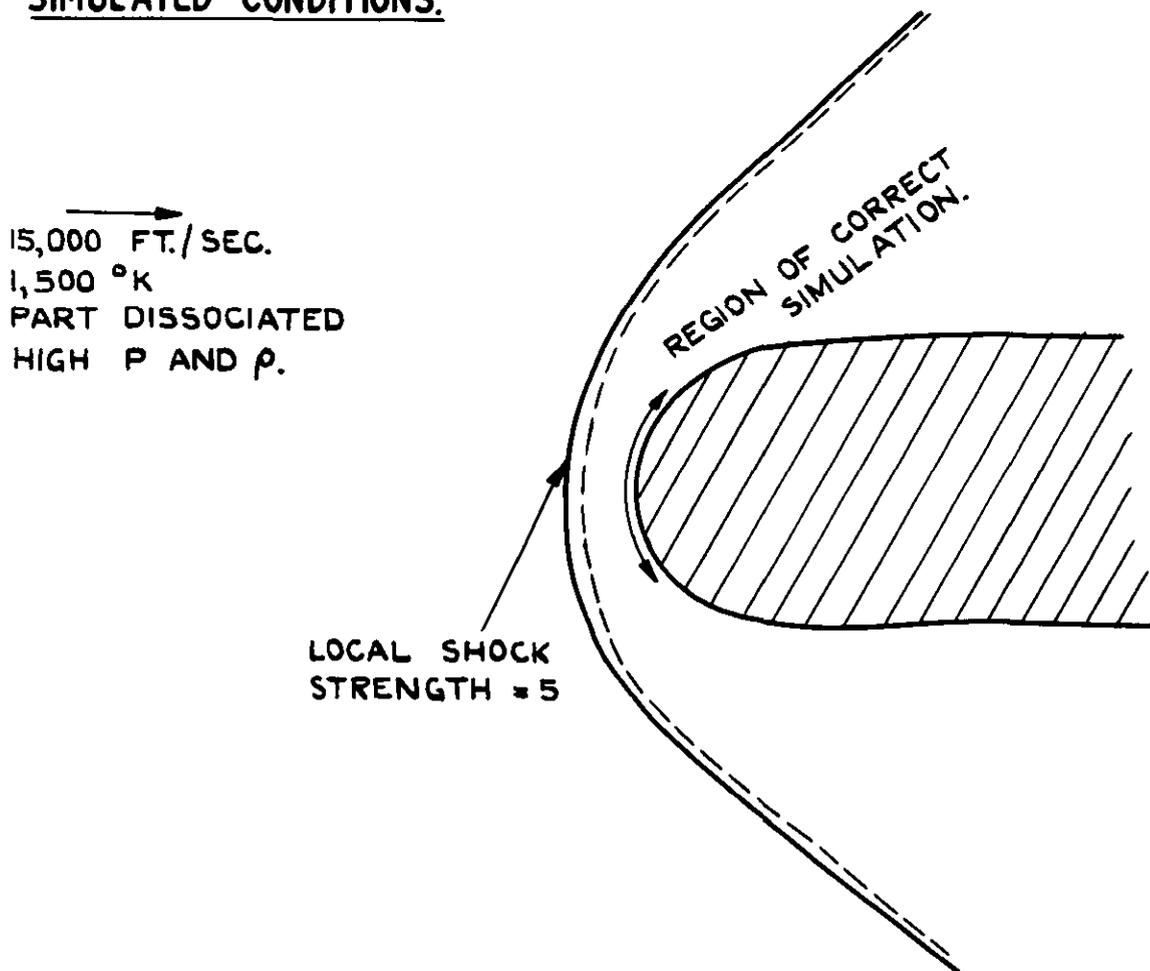


FIG. 12. SIMULATION NEAR THE NOSE OF A BLUNT BODY.

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